

# Performance Evaluation of Coherent PS-QPSK (HEXA) Modulation

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- ▶ Four-dimensional constellations
- ▶ Transmitter and receiver architecture
- ▶ Back-to-back performance
- ▶ Long-haul transmission
- ▶ Experimental demonstrations
- ▶ Conclusions



- ▶ **Four-dimensional constellations**
- ▶ Transmitter and receiver architecture
- ▶ Back-to-back performance
- ▶ Long-haul transmission
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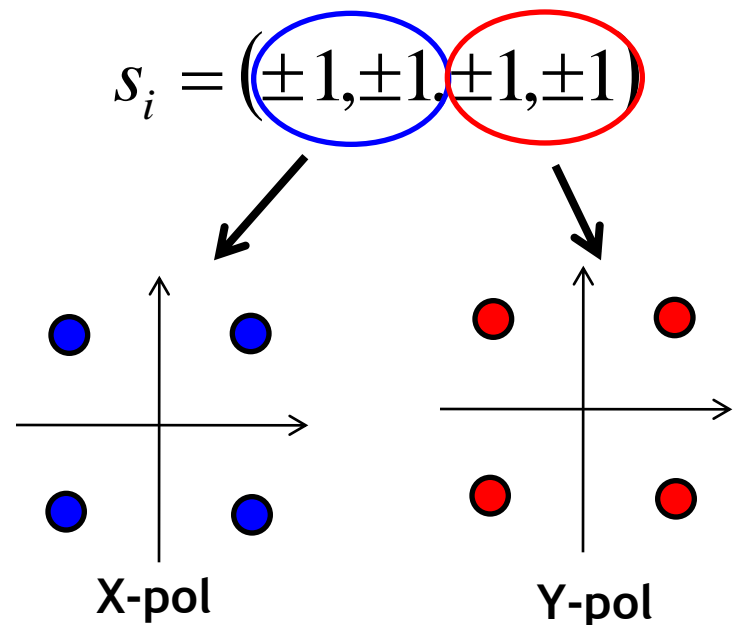
# Four-dimensional space



- ▶ Coherent detection permits to exploit the four-dimensional (4D) signal space consisting of the in-phase and quadrature components of the two polarizations of the electromagnetic field.
- ▶ Polarization-multiplexed QPSK (PM-QPSK) is an example of 4D constellation composed of 16 points.
- ▶ The constellation vectors are formed from real and imaginary parts of the electromagnetic field's X and Y polarization components.

$$\begin{array}{ll}
 s_1 = (-1, -1, -1, -1) & s_9 = (+1, -1, -1, -1) \\
 s_2 = (-1, -1, -1, +1) & s_{10} = (+1, -1, -1, +1) \\
 s_3 = (-1, -1, +1, -1) & s_{11} = (+1, -1, +1, -1) \\
 s_4 = (-1, -1, +1, +1) & s_{12} = (+1, -1, +1, +1) \\
 s_5 = (-1, +1, -1, -1) & s_{13} = (+1, +1, -1, -1) \\
 s_6 = (-1, +1, -1, +1) & s_{14} = (+1, +1, -1, +1) \\
 s_7 = (-1, +1, +1, -1) & s_{15} = (+1, +1, +1, -1) \\
 s_8 = (-1, +1, +1, +1) & s_{16} = (+1, +1, +1, +1)
 \end{array}$$

- ▶ These coordinates correspond to the vertices of a 4D “hypercube”



- ▶ PS-QPSK is 4D constellation composed of 8 points:

$$s_1 = (-2, 0, 0, 0)$$

$$s_2 = (+2, 0, 0, 0)$$

$$s_3 = (0, -2, 0, 0)$$

$$s_4 = (0, +2, 0, 0)$$

$$s_5 = (0, 0, -2, 0)$$

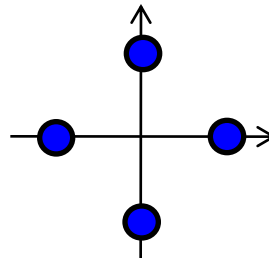
$$s_6 = (0, 0, +2, 0)$$

$$s_7 = (0, 0, 0, -2)$$

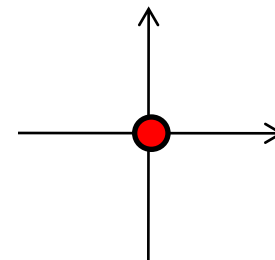
$$s_8 = (0, 0, 0, +2)$$

- ▶ Only one polarization at a time is transmitted

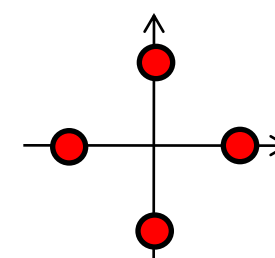
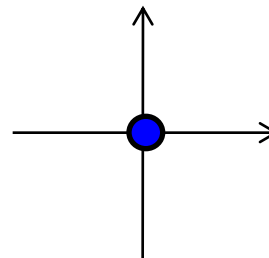
→ **polarization-switched QPSK**



X-pol



Y-pol



- ▶ These coordinates correspond to the vertices of a 4D polychoron called “hexadecachoron”

→ **HEXA**

$$s_1 = (-2, 0, 0, 0)$$

$$s_2 = (+2, 0, 0, 0)$$

$$s_3 = (0, -2, 0, 0)$$

$$s_4 = (0, +2, 0, 0)$$

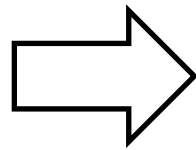
$$s_5 = (0, 0, -2, 0)$$

$$s_6 = (0, 0, +2, 0)$$

$$s_7 = (0, 0, 0, -2)$$

$$s_8 = (0, 0, 0, +2)$$

**45°  
phase  
rotation**



$$s_1 = \sqrt{2}(-1, -1, 0, 0)$$

$$s_2 = \sqrt{2}(-1, +1, 0, 0)$$

$$s_3 = \sqrt{2}(+1, -1, 0, 0)$$

$$s_4 = \sqrt{2}(+1, +1, 0, 0)$$

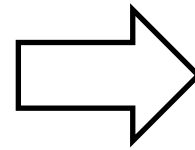
$$s_5 = \sqrt{2}(0, 0, -1, -1)$$

$$s_6 = \sqrt{2}(0, 0, -1, +1)$$

$$s_7 = \sqrt{2}(0, 0, +1, -1)$$

$$s_8 = \sqrt{2}(0, 0, +1, +1)$$

**45°  
Polarization  
rotation**



$$s_1 = (-1, -1, -1, -1)$$

$$s_2 = (-1, -1, +1, +1)$$

$$s_3 = (-1, +1, -1, +1)$$

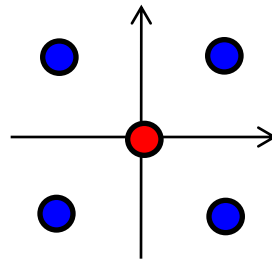
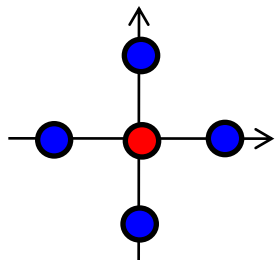
$$s_4 = (-1, +1, +1, -1)$$

$$s_5 = (+1, +1, +1, +1)$$

$$s_6 = (+1, +1, -1, -1)$$

$$s_7 = (+1, -1, +1, -1)$$

$$s_8 = (+1, -1, -1, +1)$$



**Sub-set of  
PM-QPSK points**

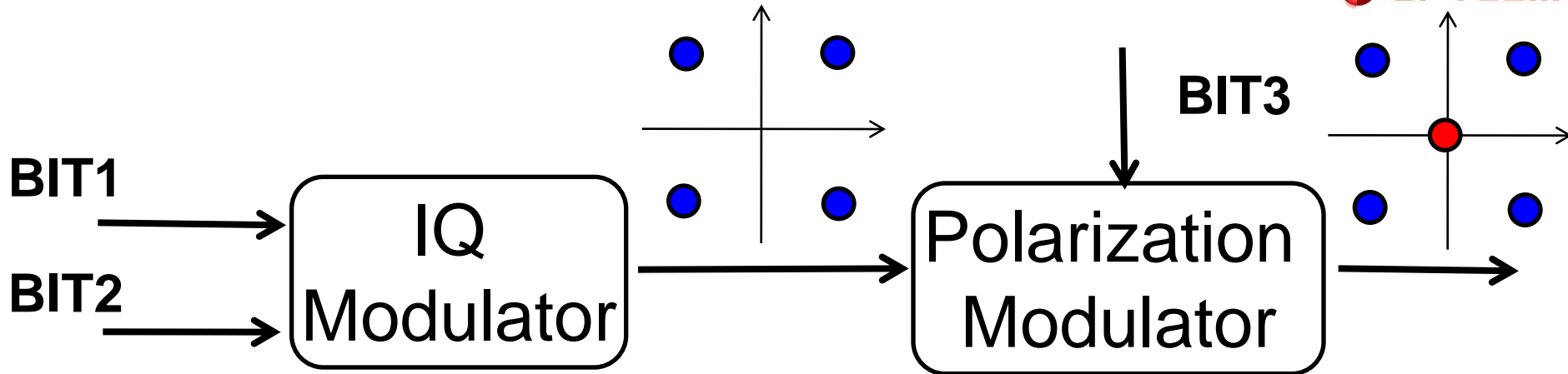
- ▶ PS-QPSK was firstly introduced in 1991:
  - ▶ *S. Betti et al., “A novel multilevel coherent optical system: 4-quadrature signaling,” J. Lightw. Tehcnol., vol. 9, no. 4, pp. 514-523, Apr. 1991.*
  
- ▶ However, only recently it was demonstrated that PS-QPSK is the most power efficient format for coherent uncoded optical systems, with an asymptotic gain of 1.76 dB w.r.t. PM-BPSK and PM-QPSK.
  - ▶ *M. Karlsson and E. Agrell, “Which is the most power efficient modulation format in optical links?”, Optics Express, vol. 17, no. 13, pp.10814-10819, Jun. 2009.*





- ▶ Four-dimensional constellations
- ▶ **Transmitter and receiver architecture**
- ▶ Back-to-back performance
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# Transmitter architecture



**Sub-set  
of  
PM-  
QPSK  
points**

$$s_1 = (-1, -1, -1, -1)$$

$$s_2 = (-1, -1, +1, +1)$$

$$s_3 = (-1, +1, -1, +1)$$

$$s_4 = (-1, +1, +1, -1)$$

$$s_5 = (+1, +1, +1, +1)$$

$$s_6 = (+1, +1, -1, -1)$$

$$s_7 = (+1, -1, +1, -1)$$

$$s_8 = (+1, -1, -1, +1)$$

**45° pol rot**

$$s_1 = \sqrt{2}(-1, -1, 0, 0)$$

$$s_2 = \sqrt{2}(-1, +1, 0, 0)$$

$$s_3 = \sqrt{2}(+1, -1, 0, 0)$$

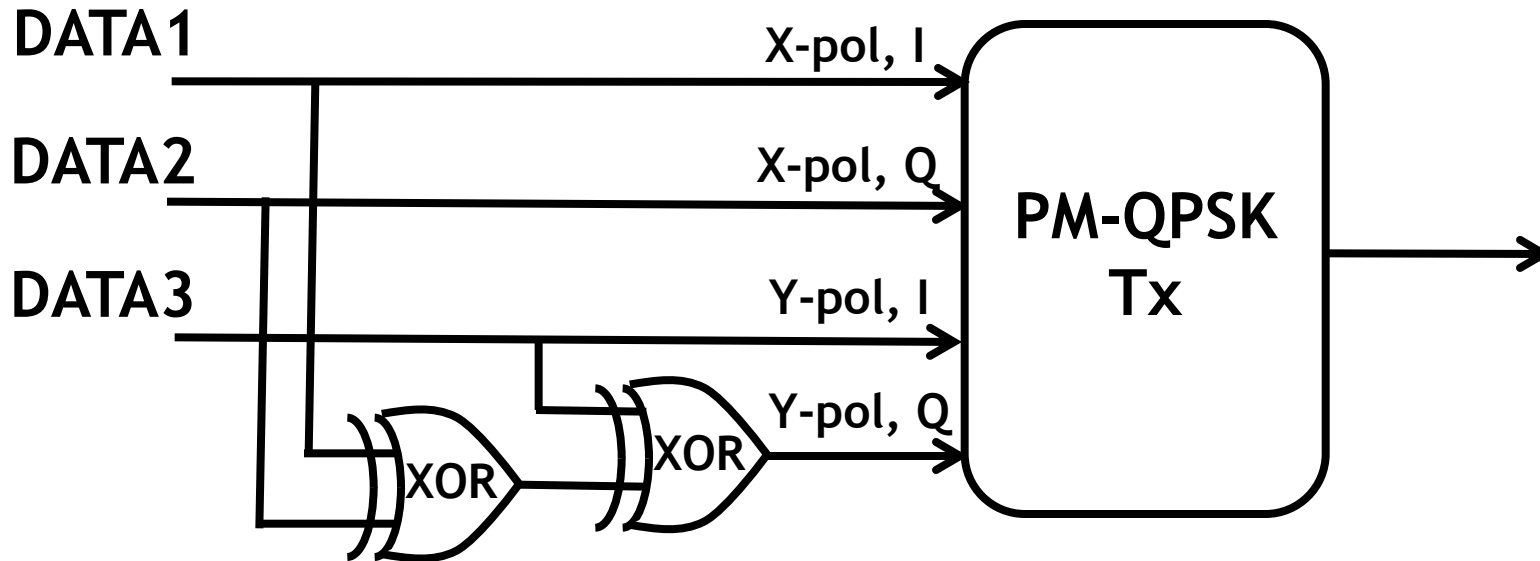
$$s_4 = \sqrt{2}(+1, +1, 0, 0)$$

$$s_5 = \sqrt{2}(0, 0, -1, -1)$$

$$s_6 = \sqrt{2}(0, 0, -1, +1)$$

$$s_7 = \sqrt{2}(0, 0, +1, -1)$$

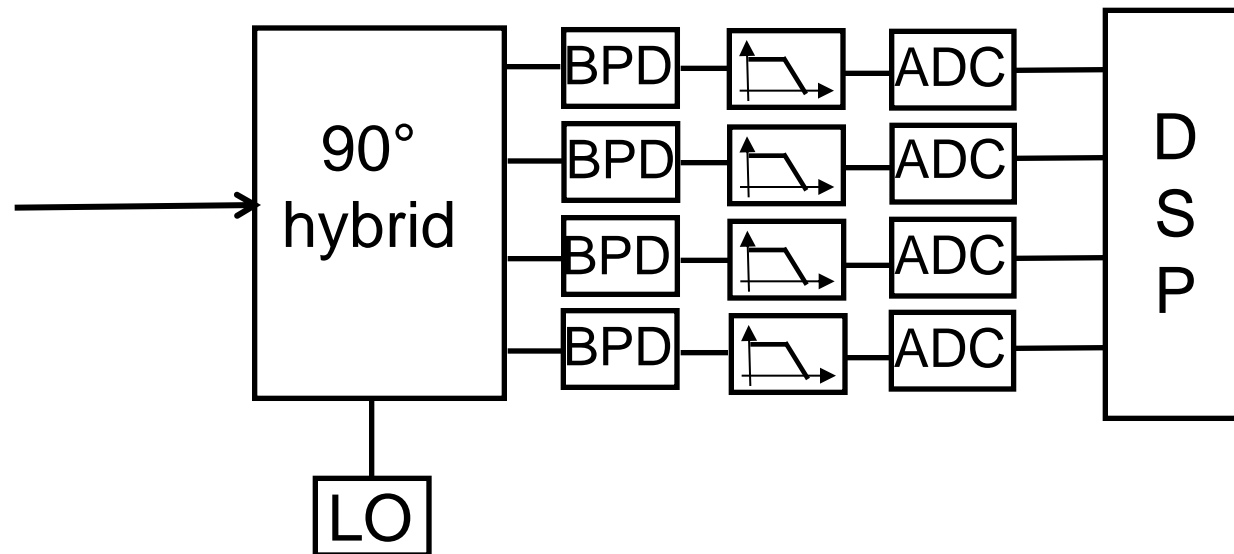
$$s_8 = \sqrt{2}(0, 0, +1, +1)$$



**Same complexity as PM-QPSK Tx (+ 2 logical gates)**

- ▶ *M. Karlsson and E. Agrell, "Which is the most power efficient modulation format in optical links?", Optics Express, vol. 17, no. 13, pp.10814-10819, 22 Jun. 2009.*

- ▶ A standard coherent Rx is used to extract the four components of the electrical field.



- ▶ The only difference w.r.t. a PM-QPSK receiver is in the DSP section.

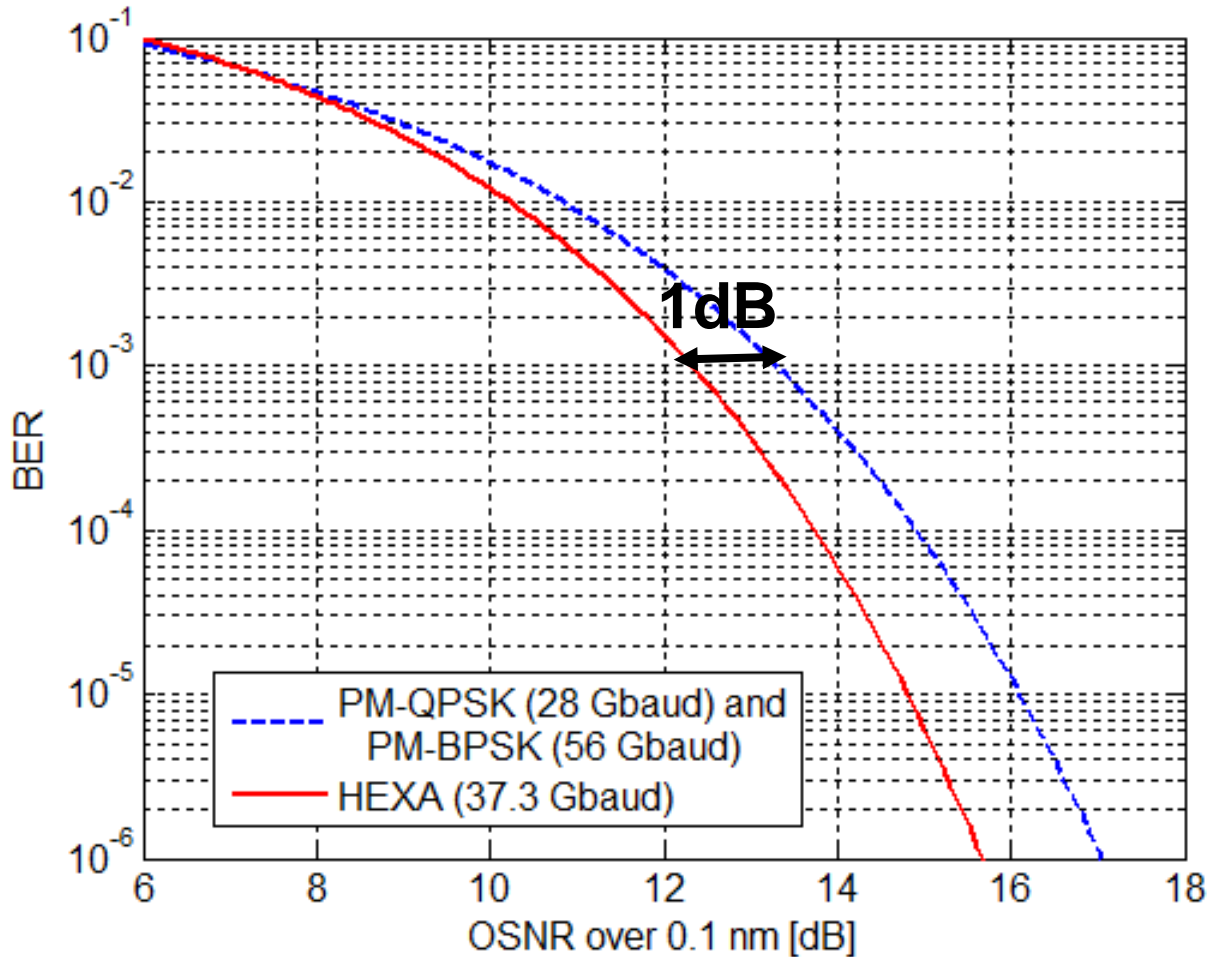


- ▶ Standard LMS algorithm
  - ▶ Initialized using a training sequence
  
- ▶ Modified CMA algorithm
  - ▶ Blind equalization
  
  - ▶ *P. Johannison et al., “Modified constant-modulus algorithm for polarization-switched QPSK”, Optics Express, vol. 19, no.8, pp. 7734-7741, 11 Apr. 2011.*
  - ▶ *D.S. Millar, S.J. Savory, “Blind adaptive equalization of polarization-switched QPSK modulation”, Optics Express, vol. 19, no.9, pp.8533-8538, 25 Apr. 2011.*
  - ▶ *P.Johannison, M. Sjödin, M. Karlsson, “A Modified CMA for PS-QPSK”, SPPCom 2011, paper SPTuB3, Jun. 2011.*



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▶  $R_b = 112 \text{ Gb/s}$

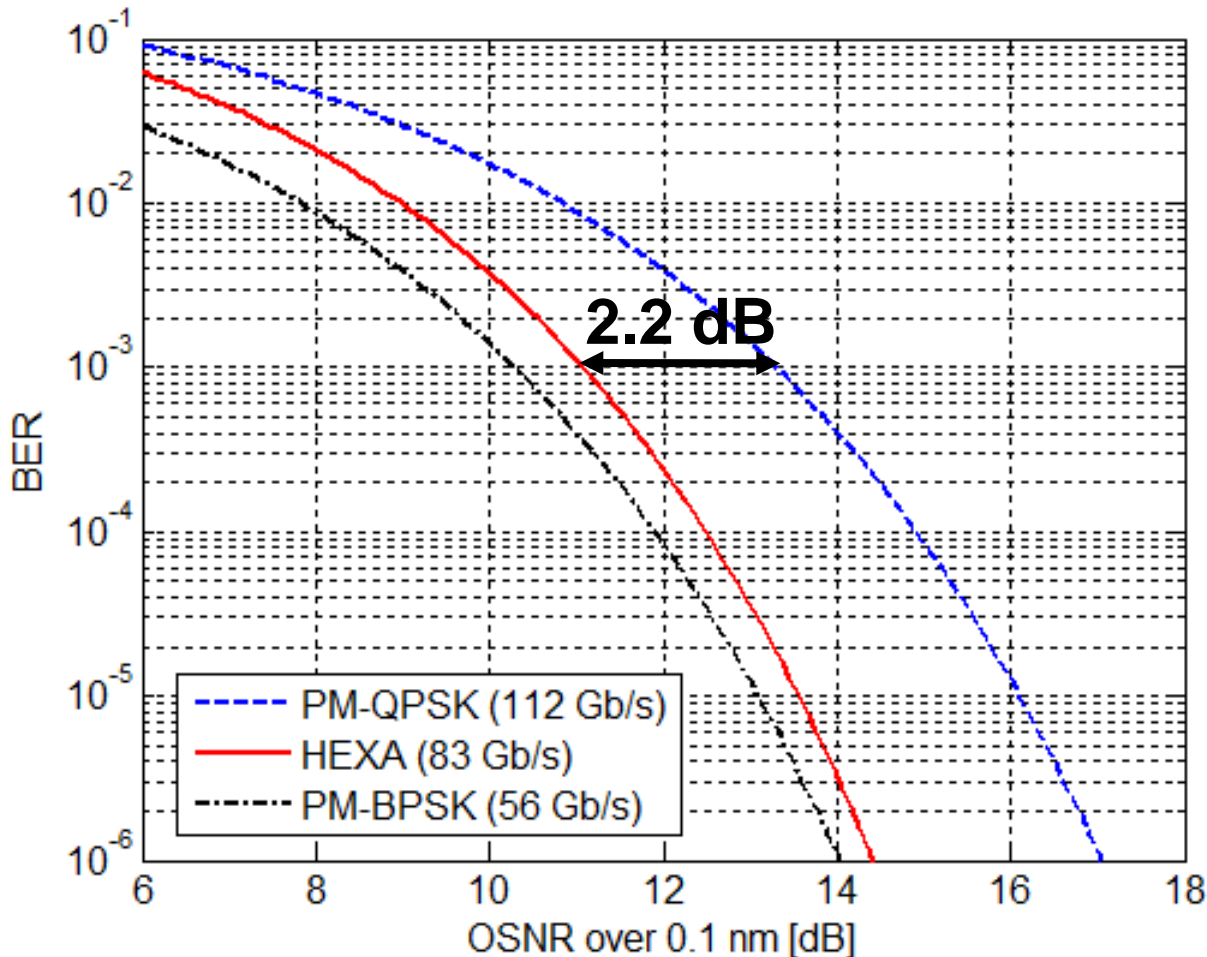


1.76-dB  
asymptotic gain  
of PS-QPSK  
(HEXA) over PM-  
QPSK

# Comparison at fixed symbol-rate

►  $R_s = 28$  Gbaud

Flexible transceiver which can switch “on-the-fly” from PM-QPSK to HEXA when channel conditions degrade.



3-dB asymptotic gain of PS-QPSK (HEXA) over PM-QPSK

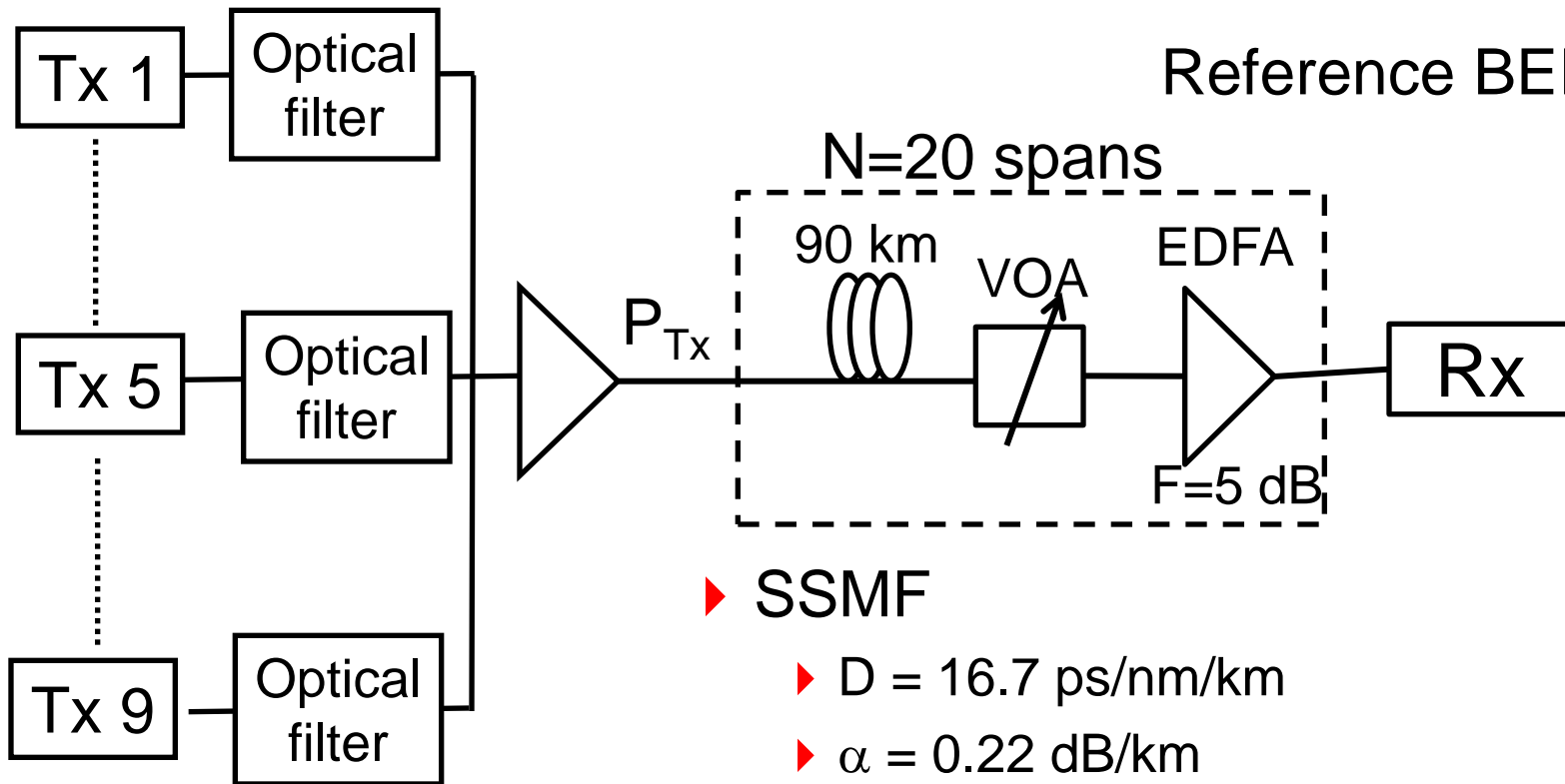


- ▶ At a reference BER of  $10^{-3}$ , the gain of PS-QPSK w.r.t. PM-QPSK is 1 dB when working at the same bit-rate and 2.2 dB when working at the same symbol-rate.
- ▶ **Is the potential gain over PM-QPSK maintained also after long-haul non-linear propagation?**



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Reference BER:  $10^{-3}$



$\Delta f = 50$  GHz

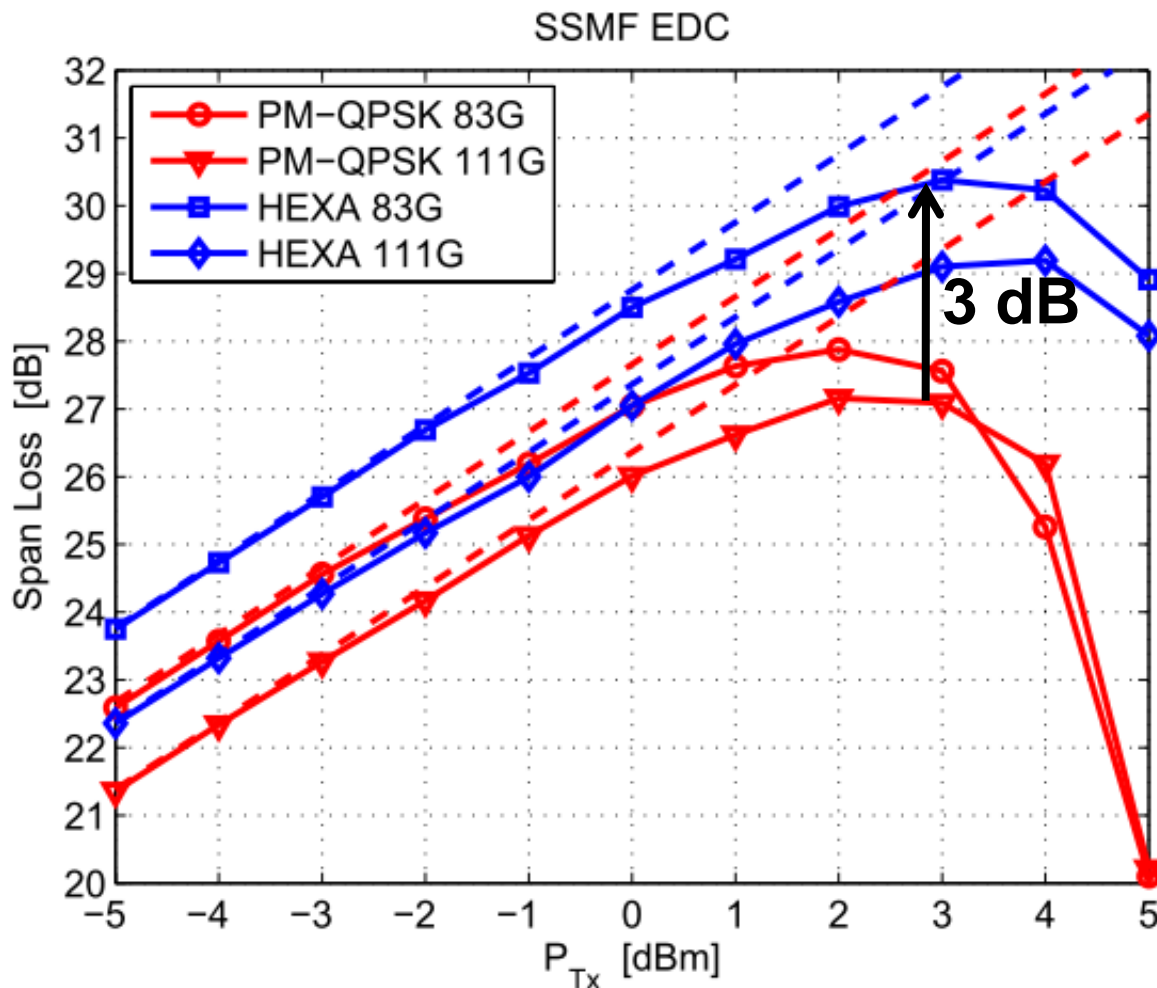
2<sup>nd</sup> order  
Supergaussian  
with 40-GHz  
bandwidth

▶ SSMF

- ▶  $D = 16.7$  ps/nm/km
- ▶  $\alpha = 0.22$  dB/km
- ▶  $\gamma = 1.3$  1/w/km

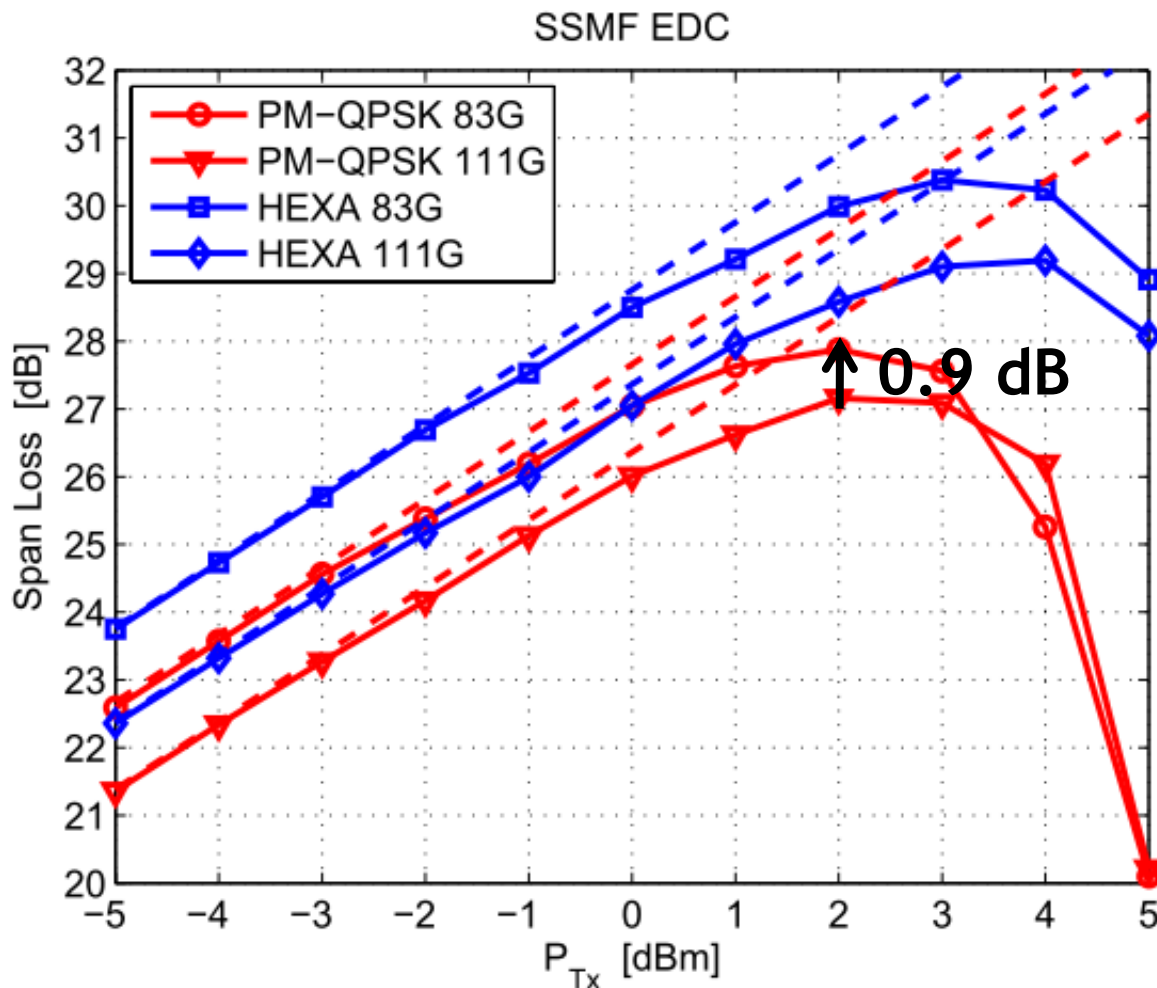
▶ NZDSF

- ▶  $D = 3.8$  ps/nm/km
- ▶  $\alpha = 0.22$  dB/km
- ▶  $\gamma = 1.5$  1/w/km



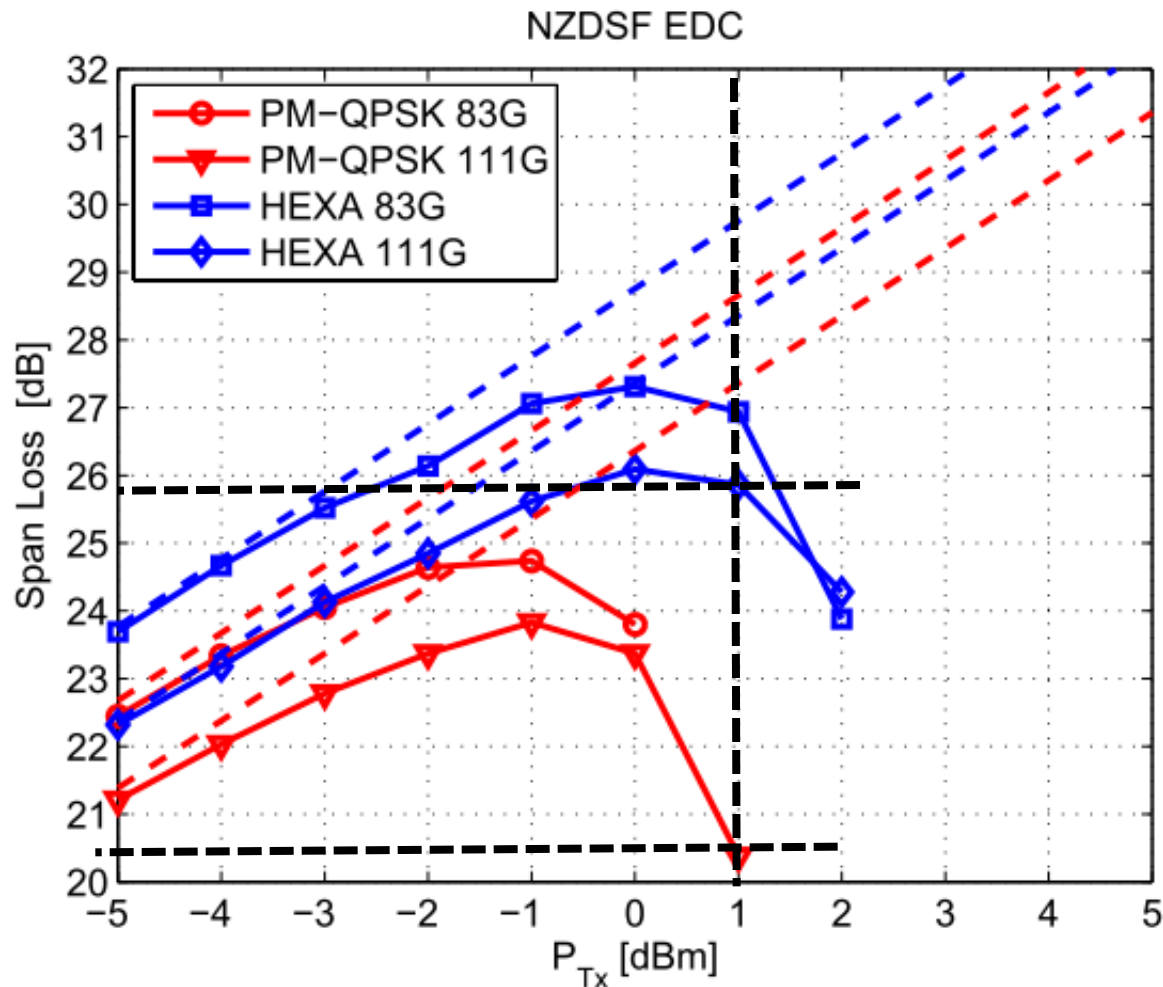
- ▶ Switching on-the-fly from 111 Gb/s PM-QPSK to 83 Gb/s PS-QPSK (HEXA) at a constant 27.75 Gbaud provides a very substantial increase in loss margin (3 dB or higher).

- ▶ *P. Poggiolini et al., "Performance evaluation of coherent WDM PS-QPSK (HEXA) accounting for non-linear fiber propagation effects", Optics Express, vol.18, no.11, May 2010, p. 11360.*



Simply reducing the PM-QPSK bit-rate down to the same 83 Gb/s does not nearly yield the same margin increase (1 dB or less is gained, only).

- ▶ *P. Poggiolini et al., "Performance evaluation of coherent WDM PS-QPSK (HEXA) accounting for non-linear fiber propagation effects", Optics Express, vol.18, no.11, May 2010, p. 11360.*



- ▶ 111 Gb/s HEXA can handle up to 1 dBm of  $P_{Tx}$ , with a tolerated span loss of almost 26 dB
- ▶ 111 Gb/s PM-QPSK, at the same launch power, is heavily impacted by non-linearity and its tolerated span loss is only about 20.5 dB.

- ▶ *P. Poggiolini et al., "Performance evaluation of coherent WDM PS-QPSK (HEXA) accounting for non-linear fiber propagation effects", Optics Express, vol.18, no.11, May 2010, p. 11360.*



# Non-linear propagation analytical models

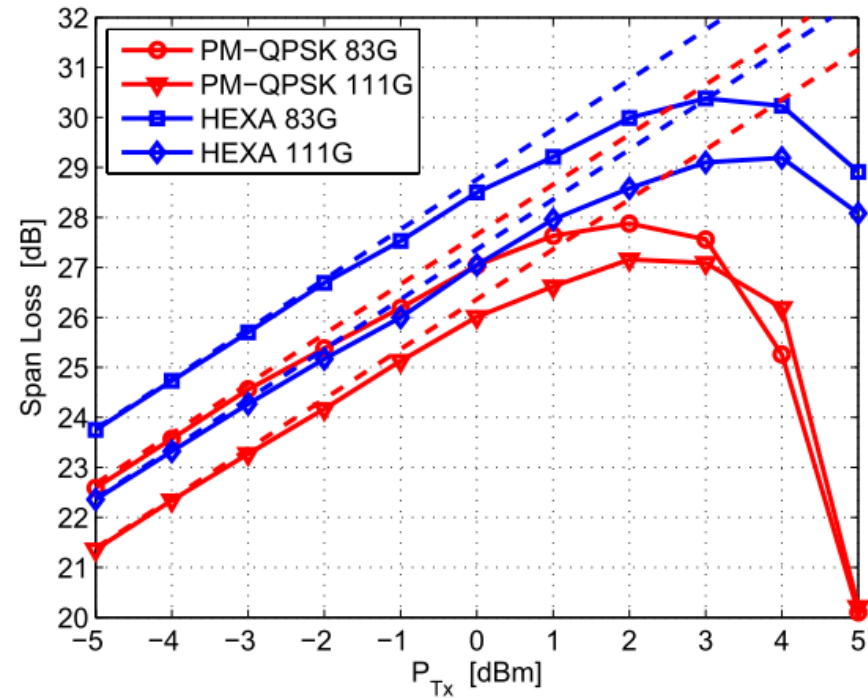


- ▶ The simulations required to obtain the results shown in previous slides took the equivalent of several months of single high-performance CPU time.
- ▶ In order to further investigate the performance of PS-QPSK, we resorted to an analytical model which has been proven to accurately predict the performance of uncompensated coherent optical systems.
- ▶ *P. Poggiolini et al., “A simple and accurate model for non-linear propagation effects in uncompensated coherent transmission links”, ICTON 2011, paper We.B1.3, Stockholm, 26-29 June 2011.*

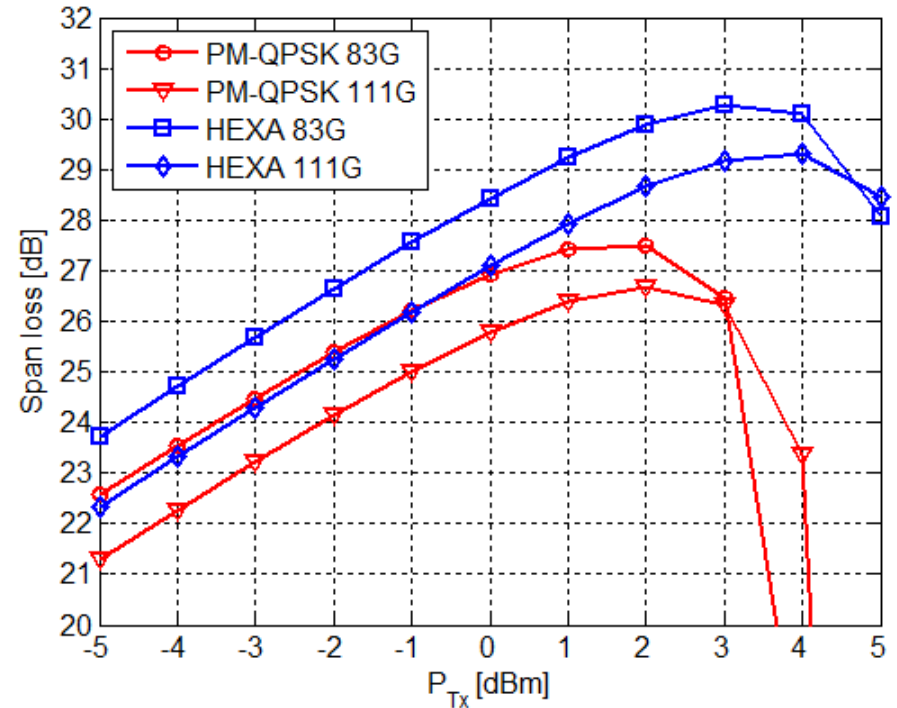
## Monte-Carlo simulations

## Analytical model

SSMF EDC



SSMF EDC



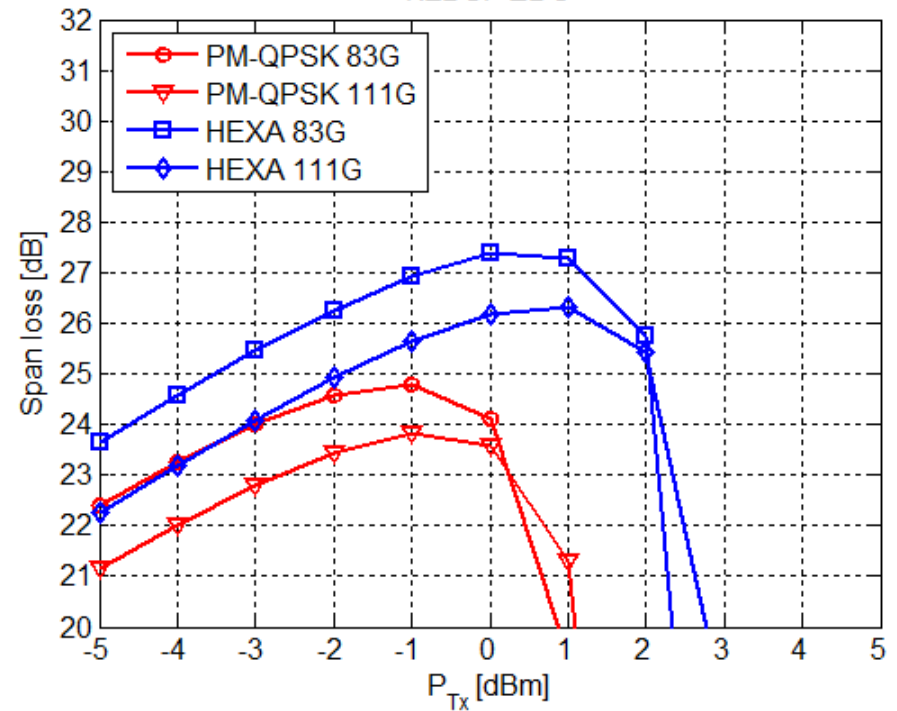
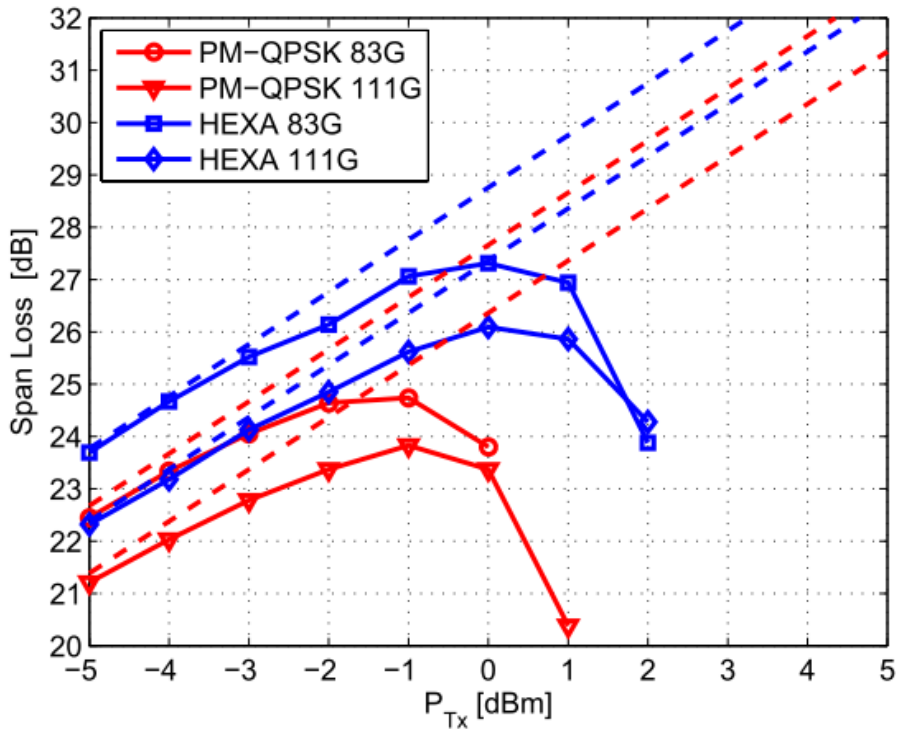


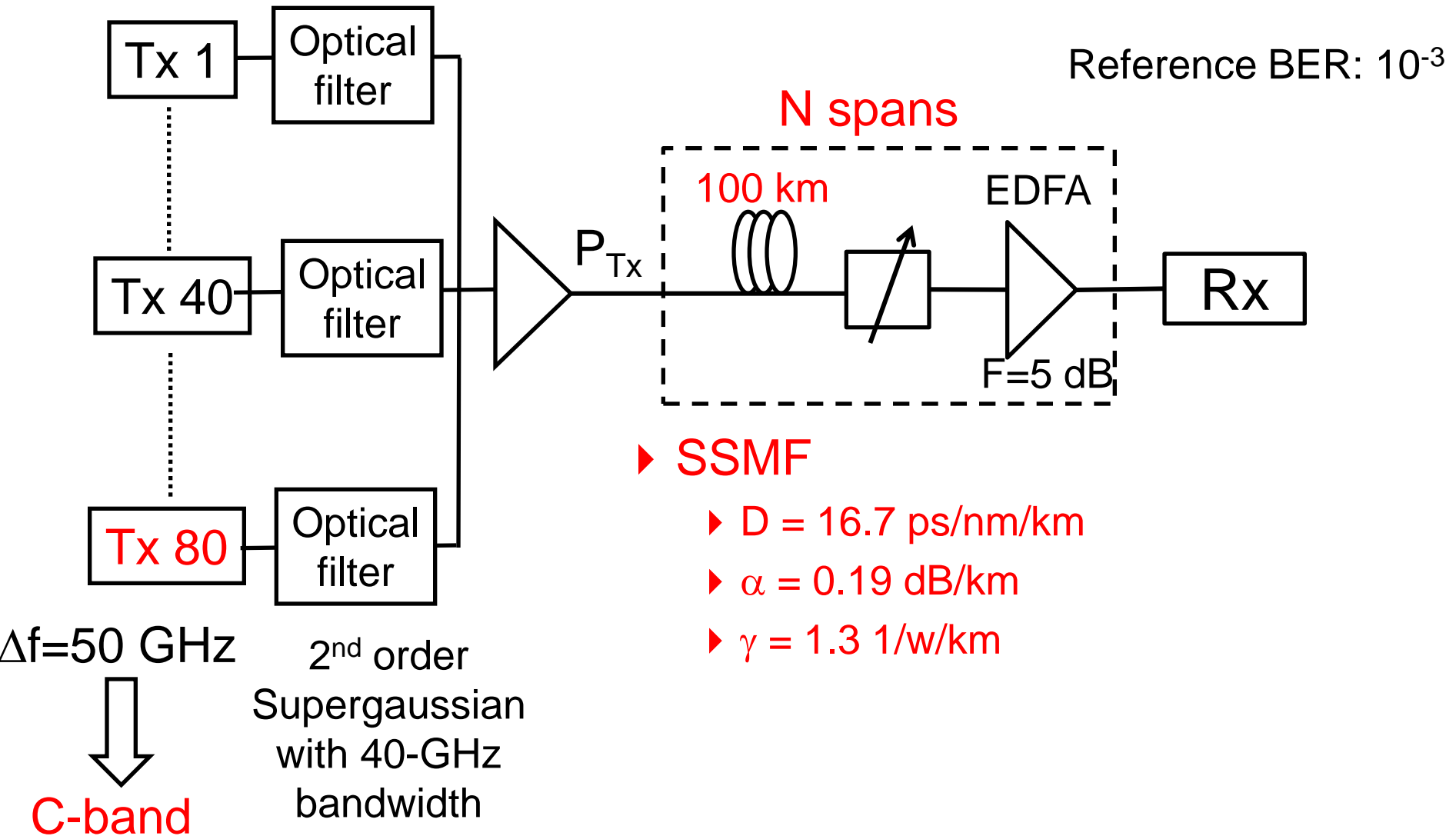
## Monte-Carlo simulations

## Analytical model

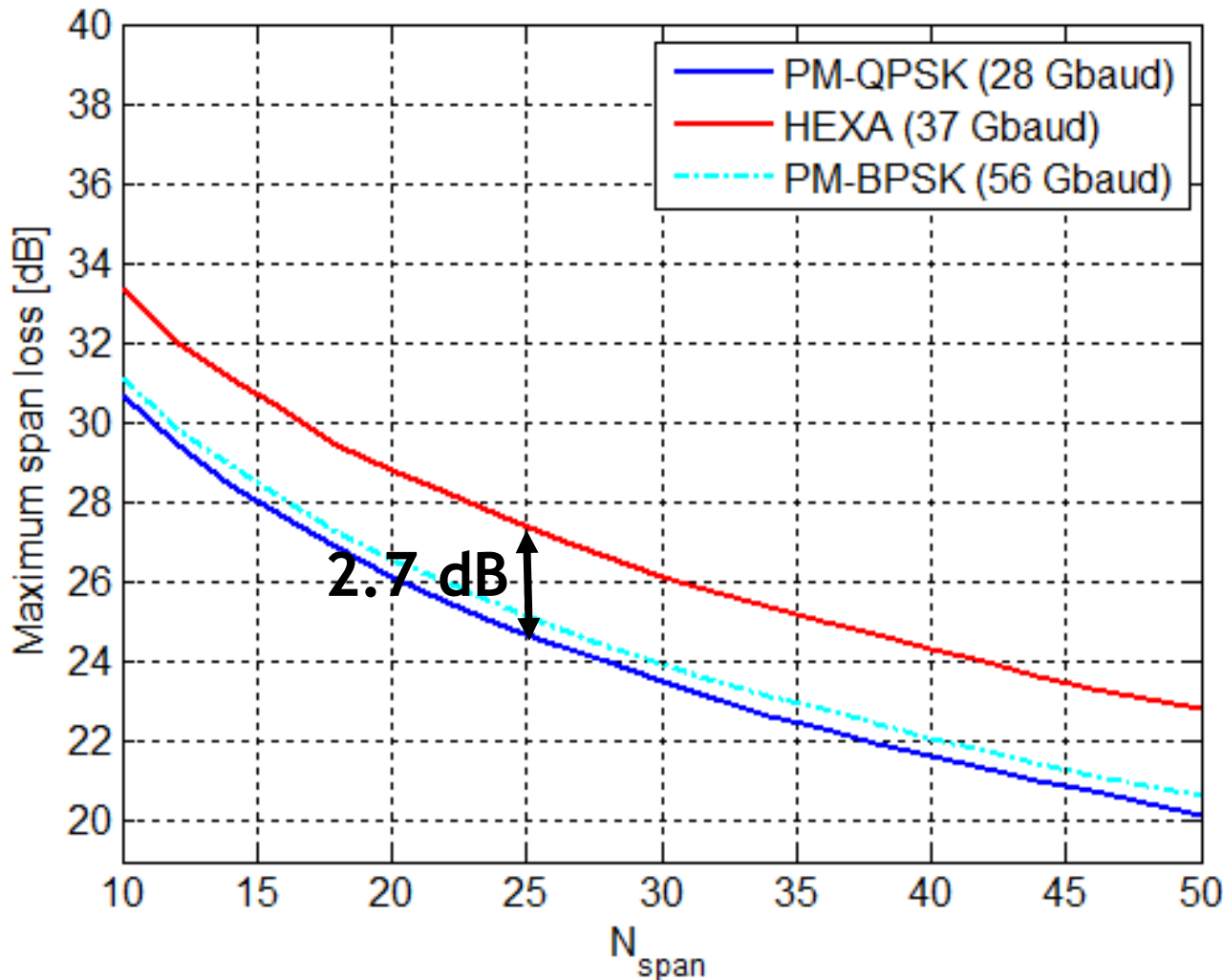
NZDSF EDC

NZDSF EDC



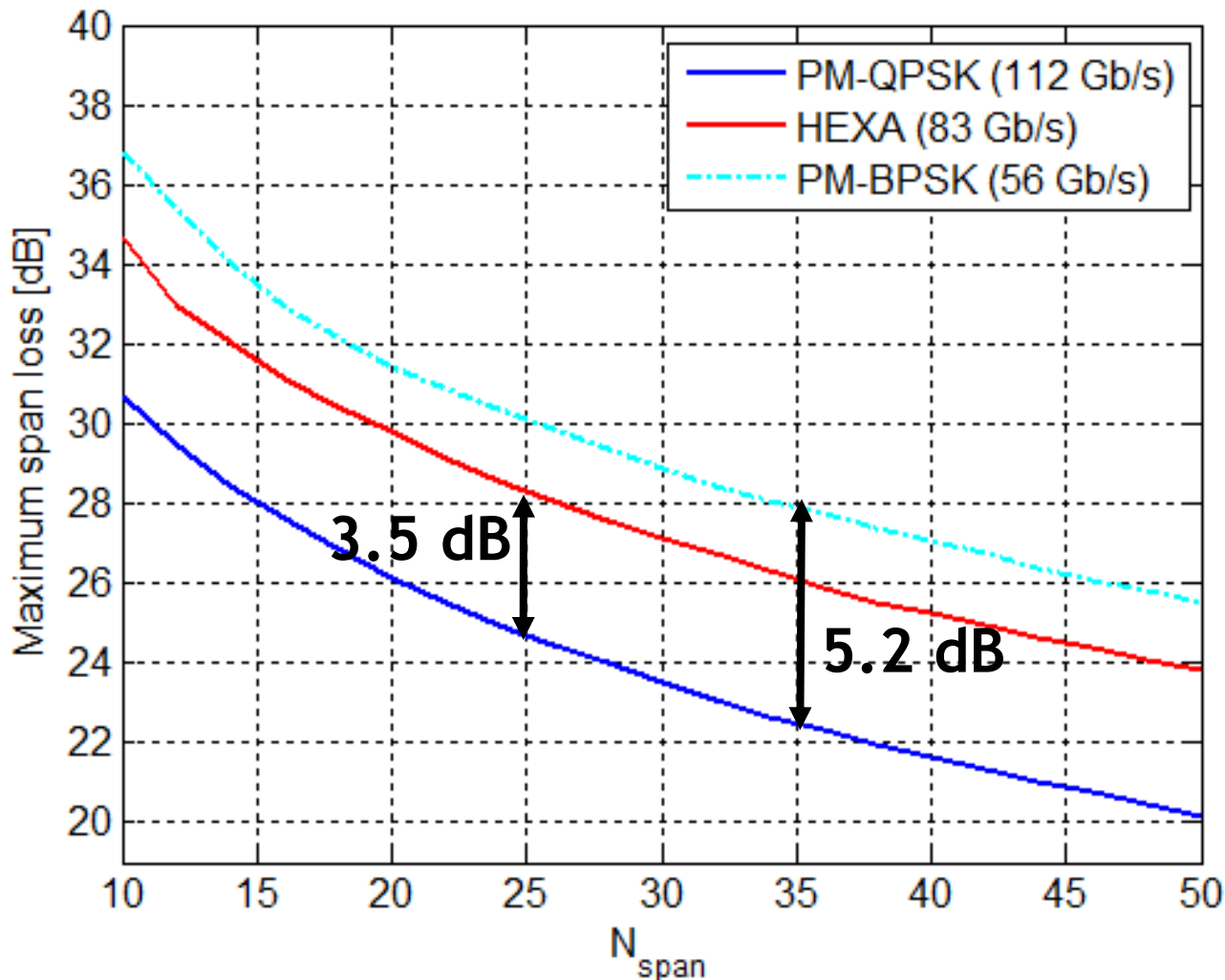


## ▶ 112 Gb/s



- ▶ The gain of PS-QPSK (HEXA) over PM-QPSK is independent of the transmission distance
- ▶ The gain has increased from 1 dB in back-to-back to 2.7 dB.

## ▶ 28 Gbaud



▶ The gain of PS-QPSK (HEXA) over PM-QPSK is independent of the transmission distance

▶ The gain has increased from 2.2 dB in back-to-back to 3.5 dB.



- ▶ Four-dimensional constellations
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- ▶ **Experimental demonstrations**
- ▶ Conclusions



# Experimental demonstrations



- ▶ Recently, experimental demonstrations of generation and transmission of PS-QPSK has started to appear, confirming analytical/simulation predictions.
- ▶ *M. Sjödin et al., “Comparison of polarization-switched QPSK and polarization-multiplexed QPSK at 30 Gbit/s”, Optics Express, vol.19, no.8, pp.7839-7846, 11 Apr. 2011.*
  - ▶ 30 Gb/s, single channel, 4x75 km SSMF
  - ▶ 0.7 dB OSNR gain over PM-QPSK at same bit-rate
  - ▶ 2.2 dB OSNR gain over PM-QPSK at same baud-rate



# Experimental demonstrations



- ▶ *D.S.Millar et al., “Generation and long-haul transmission of polarization-switched QPSK at 42.9 Gbit/s”, Optics Express, vol.19, no.10, pp.9296-9302, 9 May 2011.*
  - ▶ 42.9 Gb/s, WDM (50 GHz grid), 170x80 km SSMF (13,640 km, record length at 40 Gb/s)
  
- ▶ *L.E.Nelson et al., “Experimental comparison of coherent polarization-switched QPSK to polarization-multiplexed QPSK for 10x100 km WDM transmission”, Optics Express, vol.19, no.11, pp.10849-10856, 25 May 2011.*
  - ▶ 40.5 Gb/s, WDM (50 GHz grid), 10x100 km SSMF
  - ▶ 0.9 dB OSNR gain over PM-QPSK at same bit-rate
  - ▶ 1.6 dB higher launch power

- ▶ The obtained results indicate that PS-QPSK, besides having a better back-to-back sensitivity than PM-QPSK, is also more tolerant to non-linear propagation effects.
- ▶ Consequently, PS-QPSK emerges as an interesting option for dual-format transceivers (with fixed symbol-rate but variable bit-rate) capable to switch on-the-fly between PM-QPSK and PS-QPSK when channel propagation degrades.
- ▶ The price to pay is a 25% rate reduction, but with a gain of 2.2 dB in sensitivity and an increased tolerance to non-linear propagation effects.



# Thank you!

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