

# ASE-Noise Limit of Direct-Detection Receivers: Duobinary vs. IMDD

G. Bosco, A. Carena, V. Curri, P. Poggiolini

*Optical Communications Group - Politecnico di Torino*

*Torino - ITALY*

***OptCom@polito.it***

***www.optcom.polito.it***



**The 15th Annual Meeting of the IEEE Lasers and Electro-Optics Society**  
**10 - 14 November 2002 Glasgow, Scotland**



# Introduction

- ▶ The **optical duobinary** data-coding is a promising technology for the implementation of **ultra-dense WDM** systems with spectral efficiency close to the Nyquist limit.
- ▶ The purpose of this work is to derive, for the first time to our knowledge, the **back-to-back sensitivity** of duobinary technique in ASE-noise-limited direct detected (DD) optical systems.

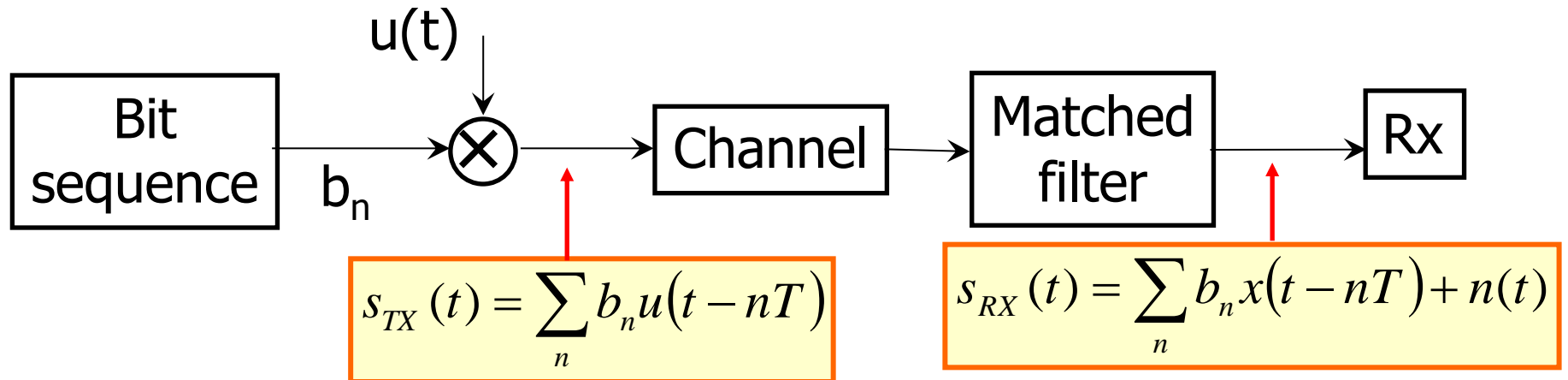


# Summary

- ▶ **Performance limit for Intensity Modulation**
- ▶ The Duobinary modulation format
- ▶ Performance limit for Duobinary with a direct-detection receiver
- ▶ A practical implementation of optical Duobinary
- ▶ Conclusions



# Intensity Modulation (IM)



## ▶ Coherent detection

$$BER = \frac{1}{2} \operatorname{erfc}(\sqrt{OSNR})$$

## ▶ Direct detection

$$BER = \frac{1}{2} \left\{ e^{-\phi} (1 + \phi) + 1 - Q_2(\sqrt{8 OSNR}, \sqrt{2\phi}) \right\}$$

Average received signal power

$$OSNR = \frac{\bar{P}_S}{2N_0 R_B}$$

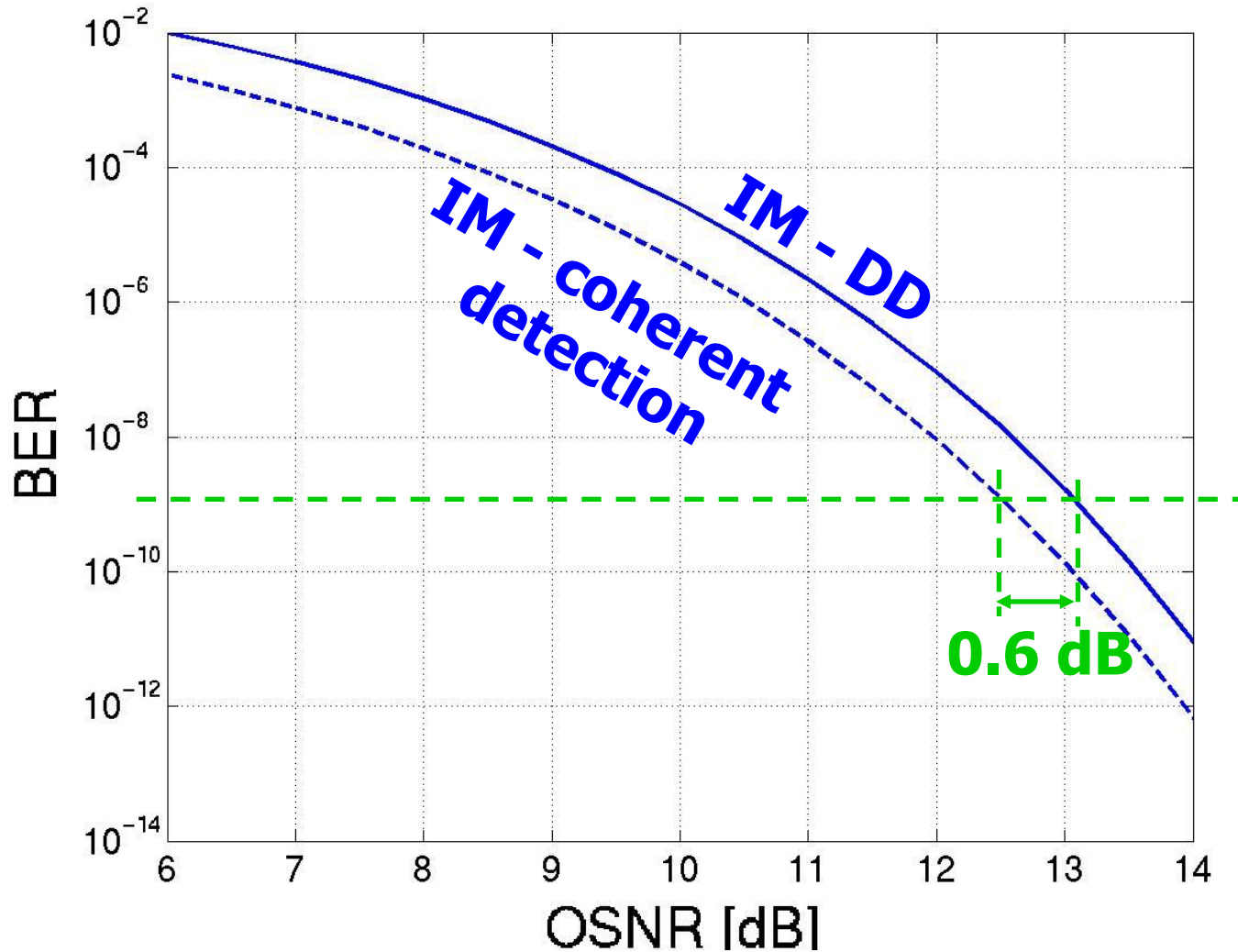
Bit-rate

ASE noise power spectral density

BER does not depend on the pulse shape



# IM: coherent vs. direct detection





# Summary

- ▶ Performance limit for Intensity Modulation
- ▶ **The Duobinary modulation format**
- ▶ Performance limit for Duobinary with a direct-detection receiver
- ▶ A practical implementation of optical Duobinary
- ▶ Conclusions



# IM vs. Duobinary

## Intensity Modulation

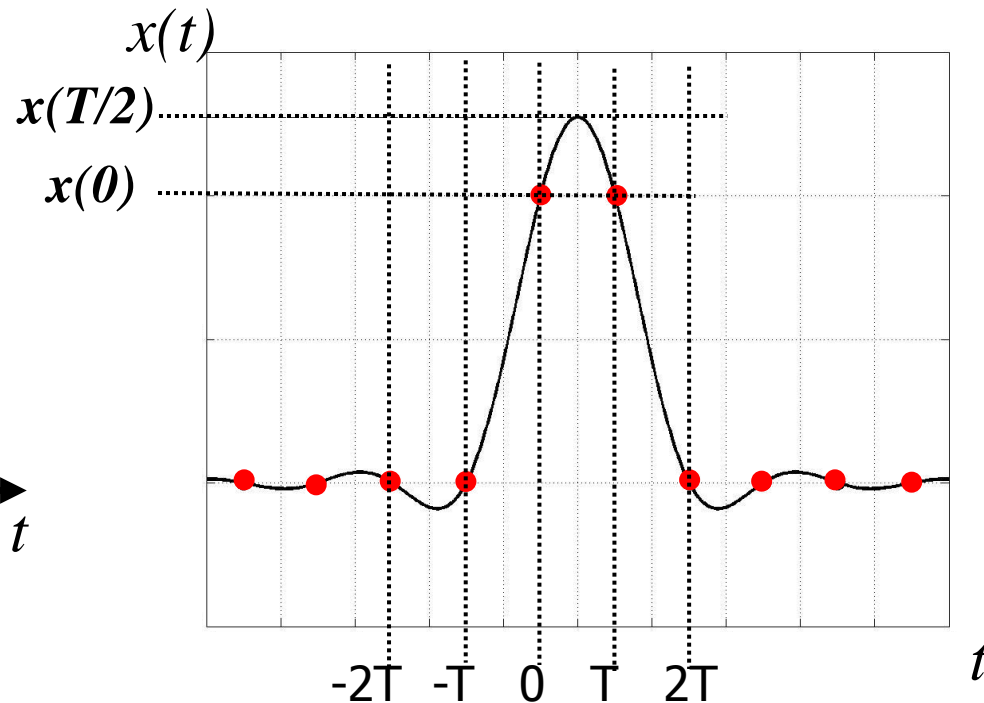
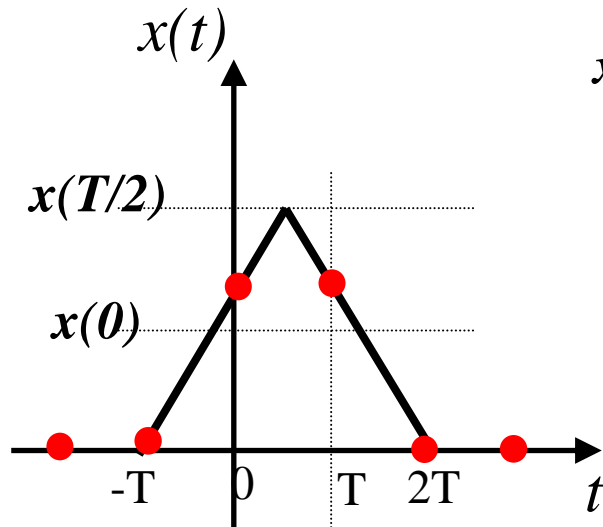
Absence of ISI:

$$x(0) \neq 0, x(nT) = 0, \forall n \neq 0$$

## Duobinary

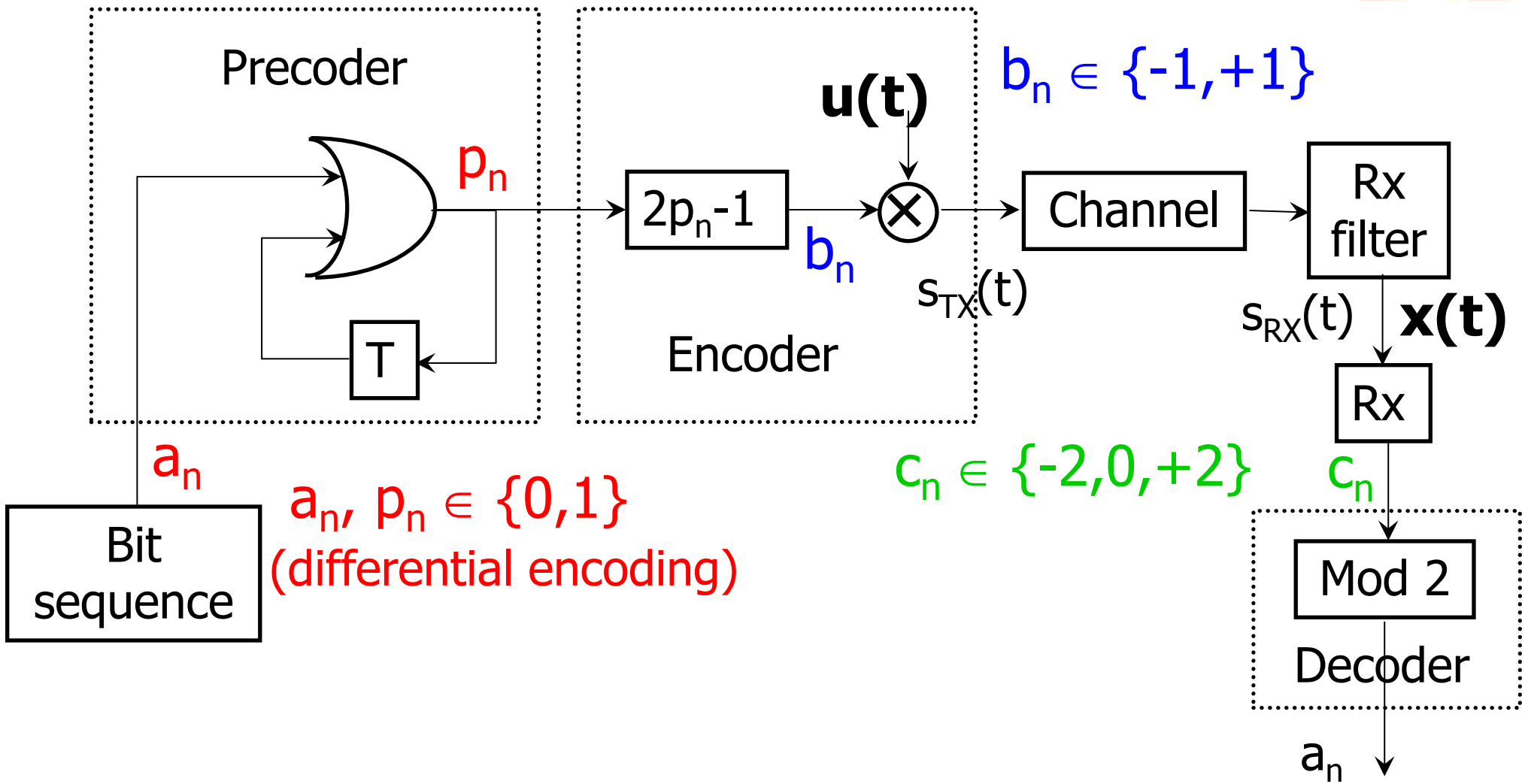
Controlled amount of ISI:

$$x(0) = x(T) \neq 0, x(nT) = 0, \forall n \neq 0,1$$





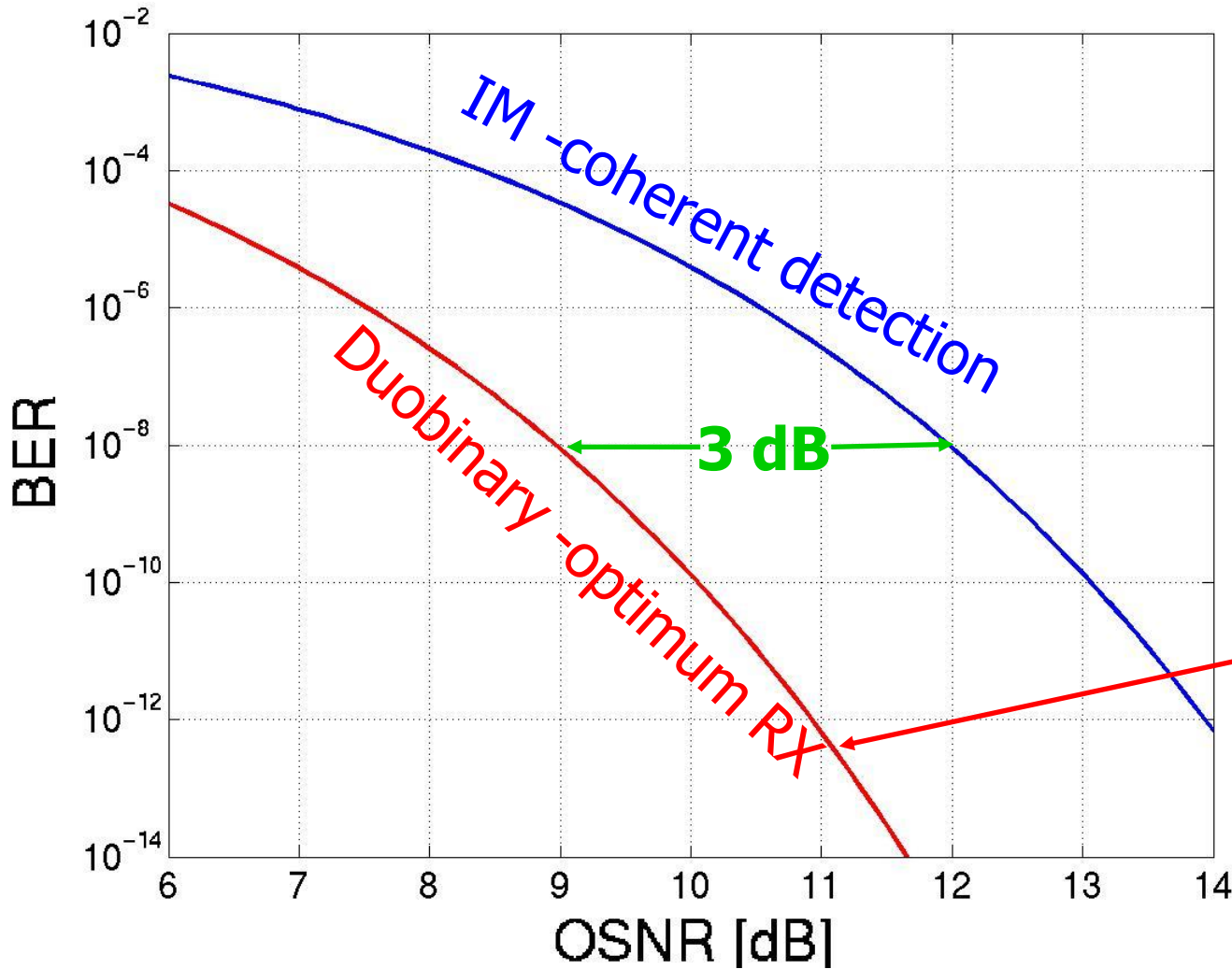
# Duobinary system schematics







# Duobinary vs. IM (optimum RX)



The optimum duobinary RX makes use of a Viterbi processor

(see J.G. Proakis, *Digital Communications*, New York, McGraw-Hill, 1989)

The BER is given by:

$$BER = \frac{1}{2} \operatorname{erfc} \left( \sqrt{2 OSNR} \right)$$



# Summary

- ▶ Performance limit for Intensity Modulation
- ▶ The Duobinary modulation format
- ▶ **Performance limit for Duobinary with a direct-detection receiver**
- ▶ A practical implementation of optical Duobinary
- ▶ Conclusions



# Duobinary received signal

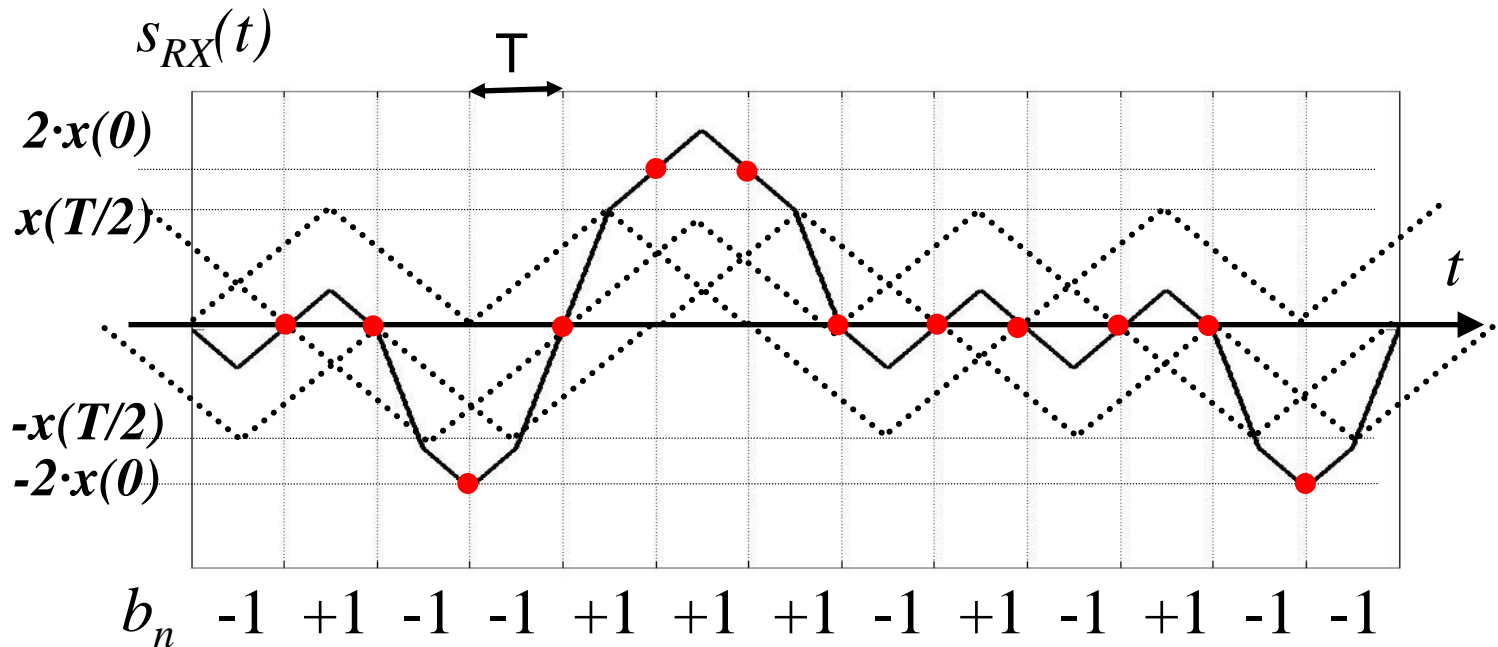
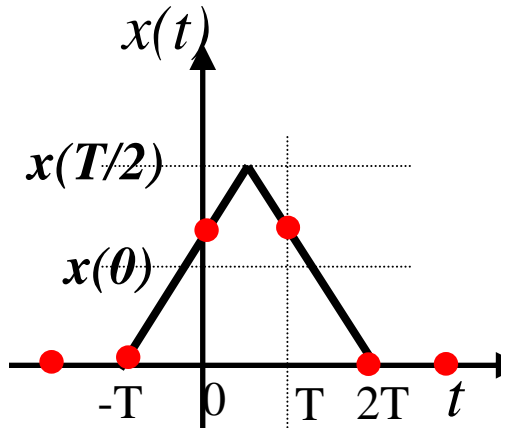
$$s_{RX}(t_{opt} + nT) = [c_n x(0) + n_r + j n_i]$$

Gaussian r.v. with

$$\sigma^2 = x\left(\frac{T}{2}\right) \frac{N_0}{2}$$

$$c_n = \begin{cases} +2 & b_n = b_{n-1} = +1 \\ 0 & b_n \neq b_{n-1} \\ -2 & b_n = b_{n-1} = -1 \end{cases}$$

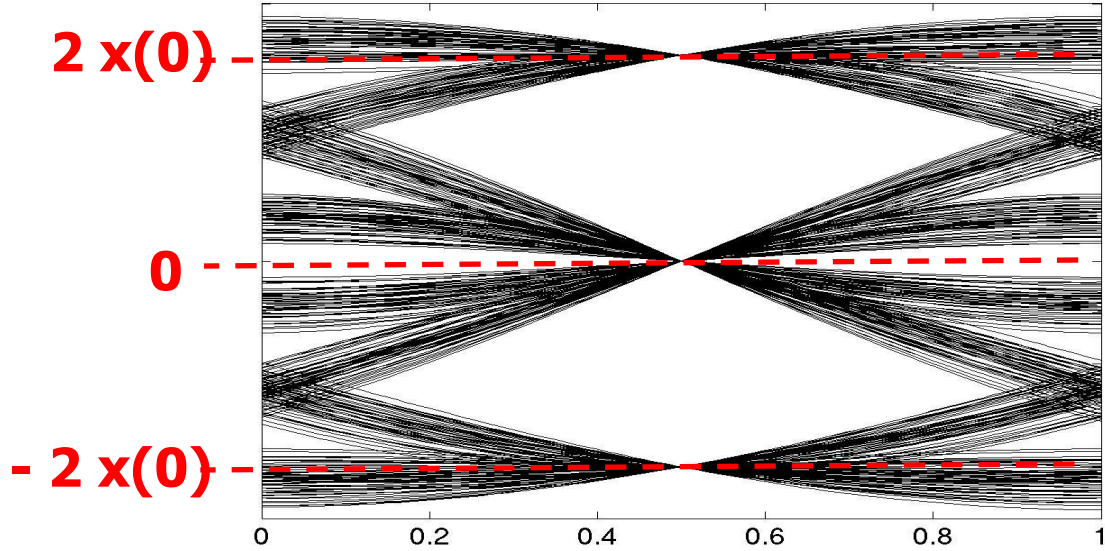
Three-level signal



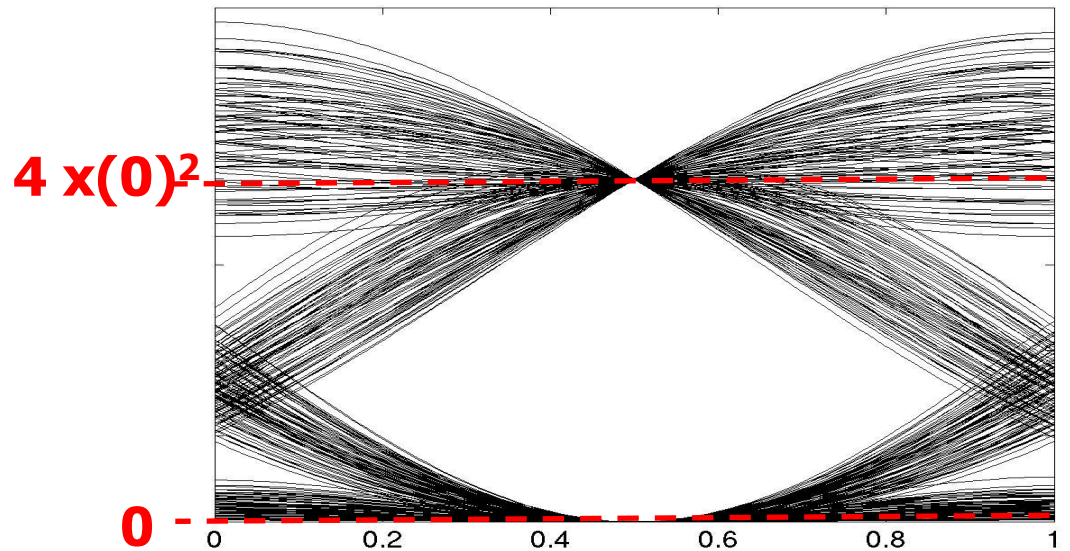


# Noiseless eye diagrams

**Before  
photodetection**



**After  
photodetection**



# Duobinary with direct-detection

- ▶ After photodetection:

$$v = \left| s_{RX} \left( t_{opt} + nT \right) \right|^2 = \left[ c_n x(0) + n_r \right]^2 + n_i^2$$

Gaussian r.v. with

$$\sigma^2 = x \left( T/2 \right) \frac{N_0}{2}$$

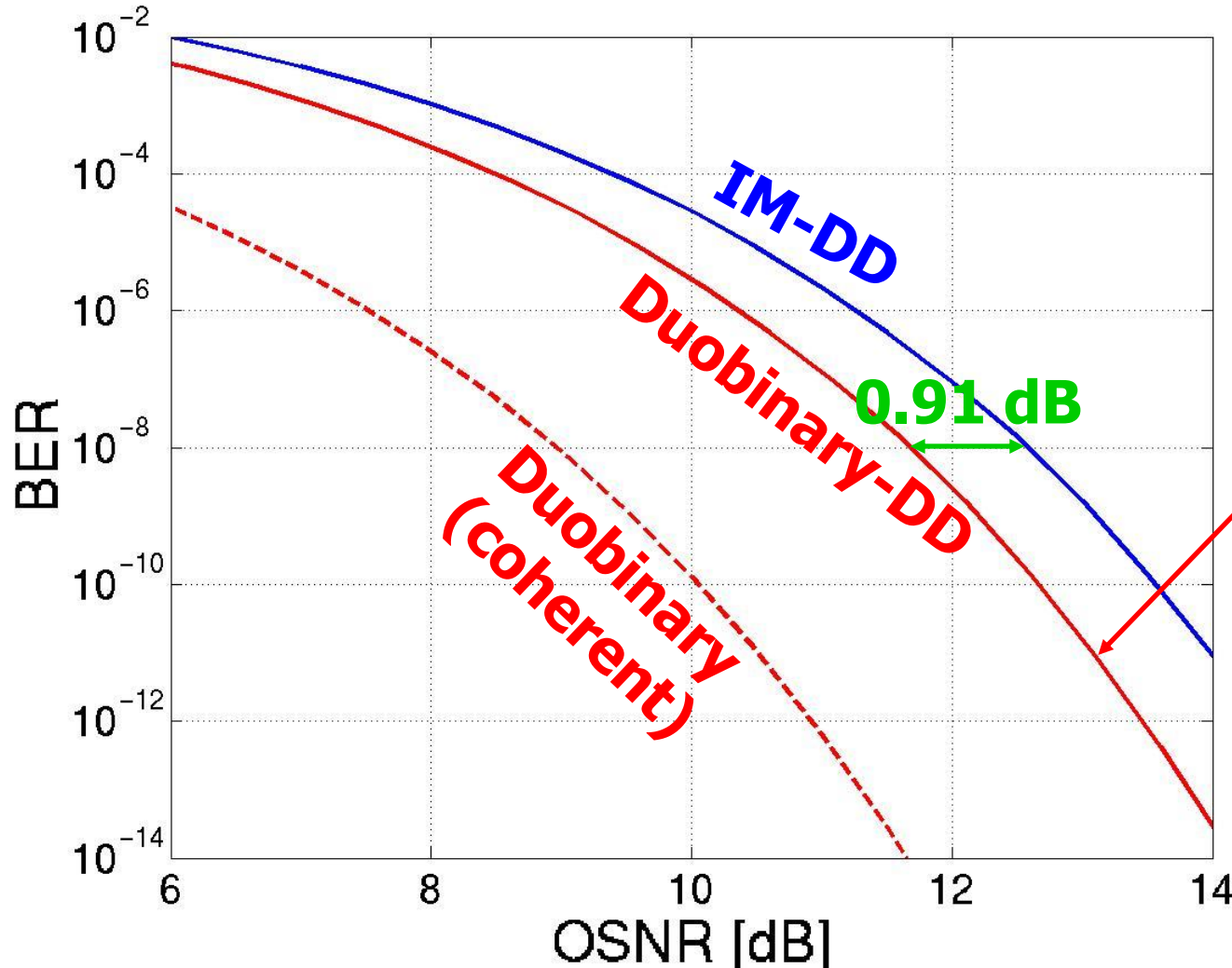
- ▶  $v$  is a Chi-square distributed r.v. with variance parameter  $\sigma^2$  and centrality parameter  $s = c_n x(0)$ .
- ▶ The BER can be analytically written as:

$$BER = \frac{1}{2} \left\{ e^{-\phi} (1 + \phi) + 1 - Q_2 \left( \frac{x(0)}{x(T/2)} \sqrt{16 OSNR}, \sqrt{2\phi} \right) \right\}$$

**The BER depends on the pulse shape !!!!**



# Direct detection: IM vs. Duobinary

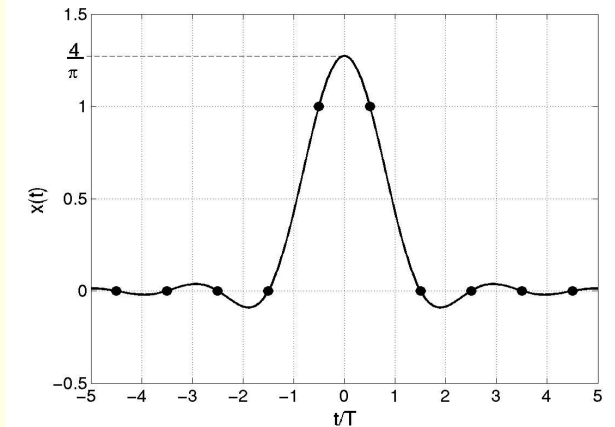


Obtained with the minimum-bandwidth pulse:

$$X(f) = 2T \cos(\pi fT)$$

$$\text{for } f \in \left[-\frac{1}{2T}, \frac{1}{2T}\right]$$

$$X(f) = 0 \text{ otherwise}$$



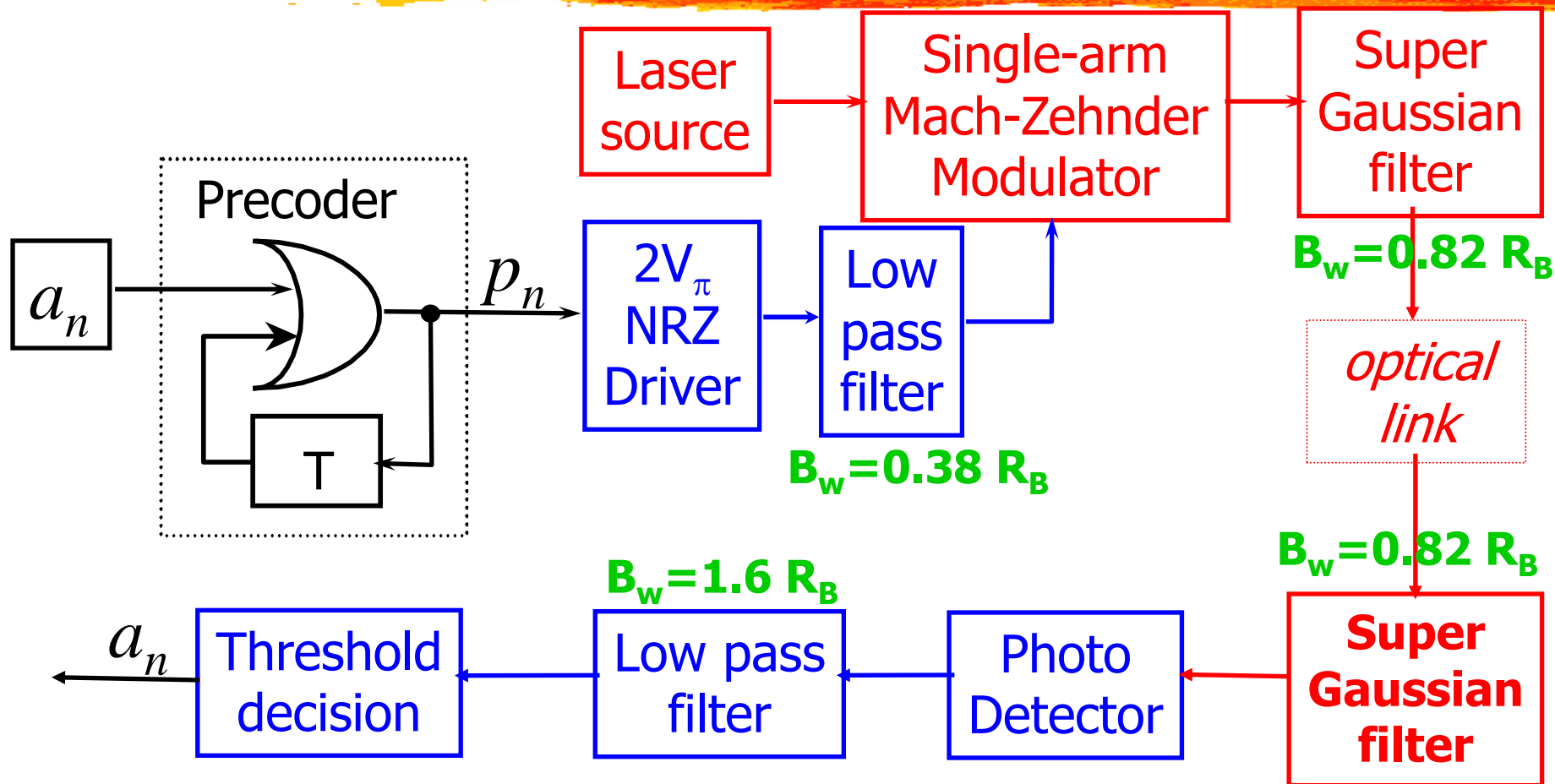


# Summary

- ▶ Performance limit for Intensity Modulation
- ▶ The Duobinary modulation format
- ▶ Performance limit for Duobinary with a direct-detection receiver
- ▶ **A practical implementation of optical Duobinary**
- ▶ Conclusions



# Practical implementation of optical duobinary



D. Penninckx et al., "The Phase-Shaped Binary Transmission (PSBT)": a new technique to transmit far beyond the chromatic dispersion limit", *IEEE Photon. Technol. Lett.*, vol. 9, no. 2, Feb. 1997.

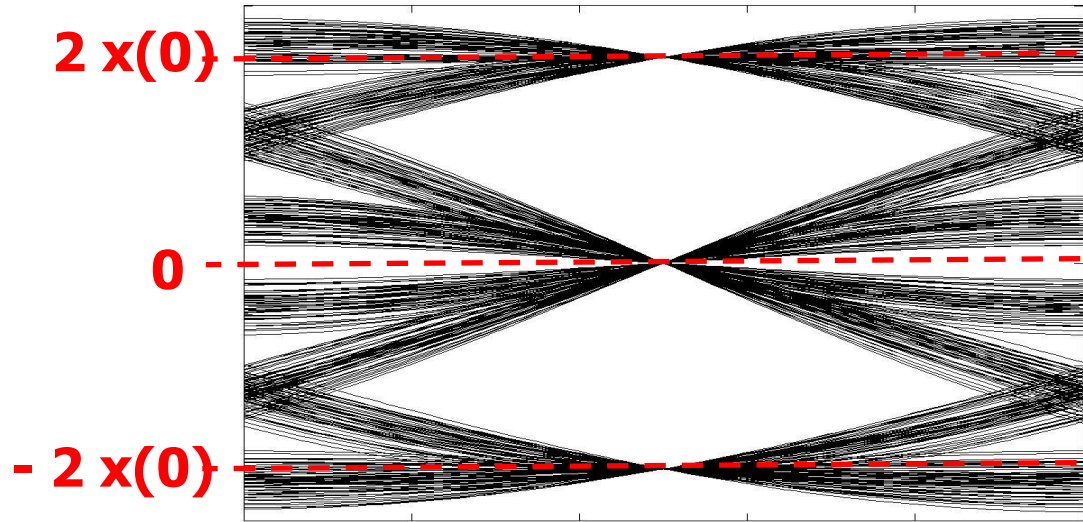




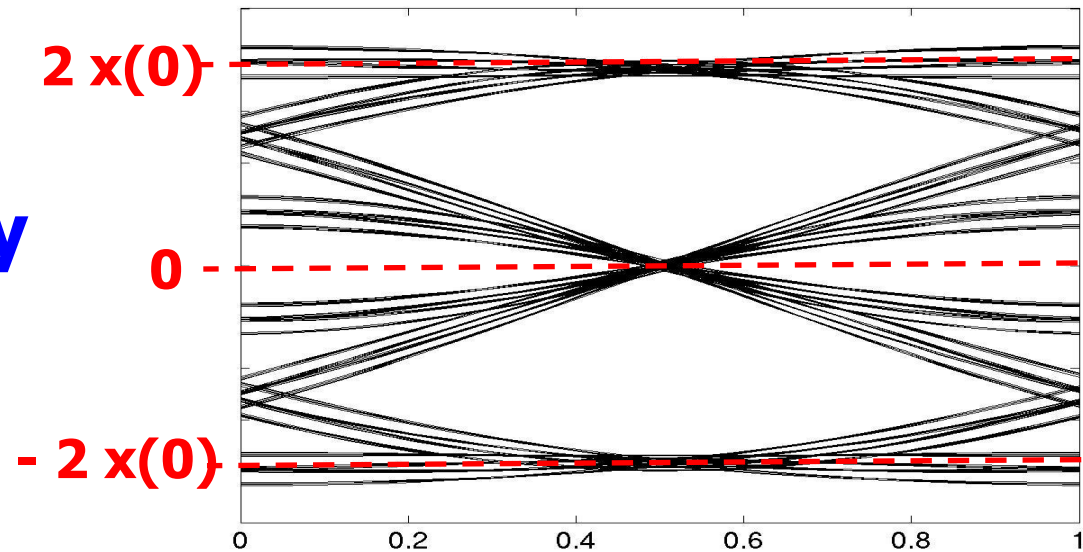
# Noiseless eye diagrams

## Matched filter with minimum bandwidth pulse

(before photodetection)

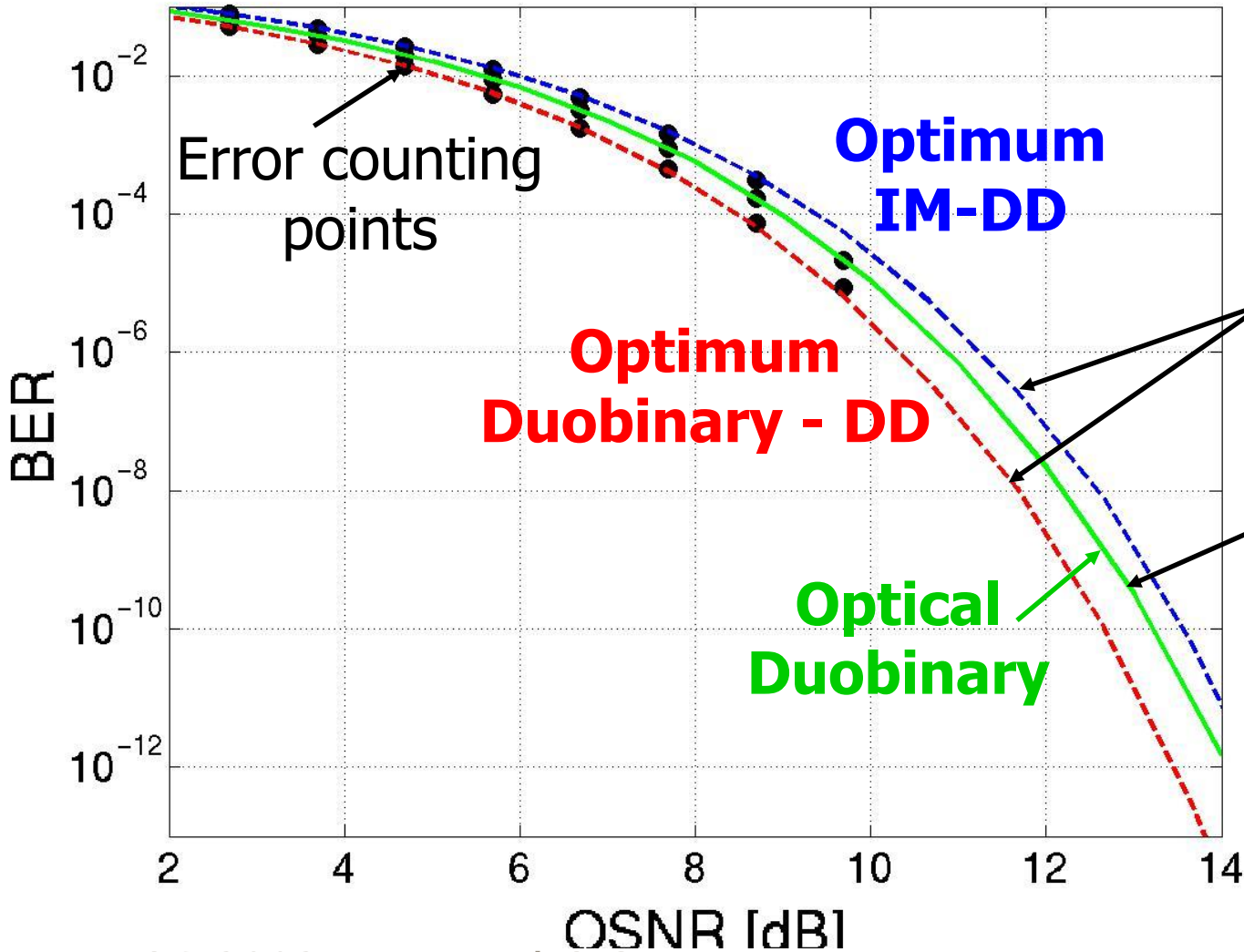


## Optical duobinary





# Performance comparison



analytical

Evaluated through simulation using the semi-analytical technique described in:

G. Bosco et al., "A novel analytical approach to the evaluation of the impact of fiber parametric gain on the bit error rate", *IEEE Trans. on Commun.*, vol. 49, no.12, pp. 2154-2163, Nov. 2001



# Summary

- ▶ Performance limit for Intensity Modulation
- ▶ The Duobinary modulation format
- ▶ Performance limit for Duobinary with a direct-detection receiver
- ▶ A practical implementation of optical Duobinary
- ▶ **Conclusions**



# Conclusions

- ▶ An expression of the BER in a back-to-back ASE noise limited optical system employing the duobinary modulation format has been derived.
- ▶ The expression of the BER for the matched-filter duobinary depends on the pulse shape.
- ▶ The back-to-back sensitivity of direct-detection duobinary is at least 0.91 dB better than the one of intensity modulation.
- ▶ Practical implementations of optical duobinary have the potential of exceeding the quantum limit of IMDD.