

# Impact of the Transmitted Signal Initial Dispersion Transient on the Accuracy of the GN-Model of Non-Linear Propagation



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- ▶ Non-linear propagation in uncompensated links can be studied using the GN-model
- ▶ GN-model ingredients:
  - ▶ Signal is Gaussian distributed
  - ▶ Nonlinear Interference is Gaussian distributed and additive
  - ▶ Nonlinear Interference is perturbative
- ▶ First ingredient is not verified at system input: it takes some accumulated dispersion to turn the signal into Gaussian noise
- ▶ This work investigates the error introduced by the Initial Dispersion Transient (IDT) with respect to prediction of the GN-model



- ▶ A quick recap of the GN-model
- ▶ NLI estimation technique
- ▶ Simulation setup
  - ▶ Reference system description
- ▶ Results
  - ▶ Impact on system performance prediction
- ▶ Conclusions



$$G_{NLI}(f) = \frac{16}{27} \gamma^2 \cdot \int_{-\infty-\infty}^{+\infty+\infty} \int G_{Tx}(f_1) G_{Tx}(f_2) G_{Tx}(f_1 + f_2 - f) \cdot \left| \frac{1 - e^{-2\alpha L_S} e^{j4\pi^2 |\beta_2| L_S (f_1 - f)(f_2 - f)}}{2\alpha - j4\pi^2 |\beta_2| (f_1 - f)(f_2 - f)} \right|^2 \cdot \frac{\sin^2(2N_S \pi^2 (f_1 - f)(f_2 - f) |\beta_2| L_S)}{\sin^2(2\pi^2 (f_1 - f)(f_2 - f) |\beta_2| L_S)} df_1 df_2$$

$N_s$

$$\sigma_{NLI}^2 = \eta P_{ch}^3$$

Coherent NLI accumulation

$$\sigma_{NLI}^2 = \sigma_{NLI}^{2(1span)} \cdot N_s^{1+\varepsilon}$$

Incoherent NLI accumulation

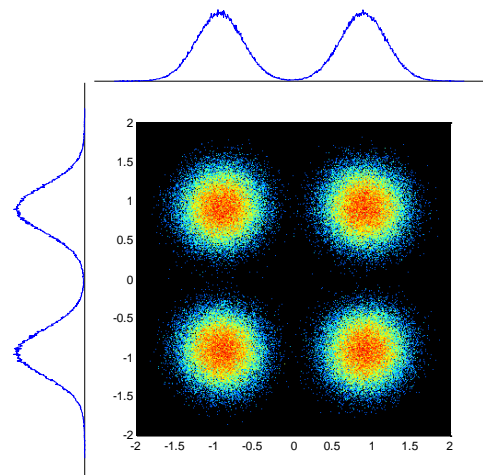
$$\sigma_{NLI}^2 = \sigma_{NLI}^{2(1span)} \cdot N_s$$

- ▶ NLI variance was estimated directly on the scattering diagram by averaging  $\sigma$  of all points
- ▶ Noiseless simulations with:
  - ▶ non-linearity turned on  $\rightarrow \sigma_{tot}^2$
  - ▶ non-linearity turned off  $\rightarrow \sigma_{lin}^2$
- ▶ The NLI variance was found as:

$$\sigma_{NLI}^2 = \sigma_{tot}^2 - \sigma_{lin}^2$$

and  $\eta$  as

$$\eta = \frac{\sigma_{NLI}^2}{P_{ch}^3}$$





# Reference system: Tx & Rx

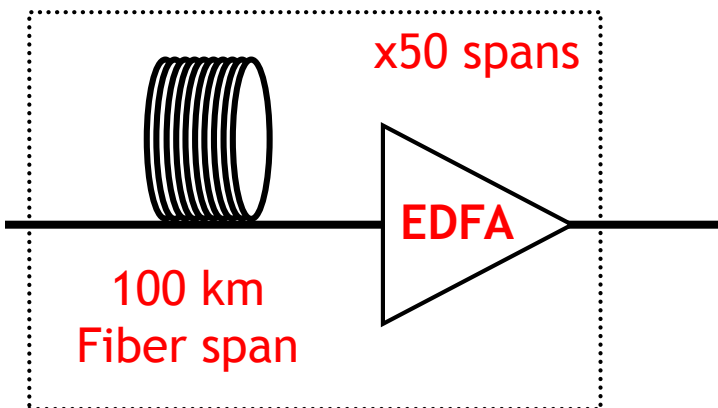


## TRANSMITTER

- ▶  $R_S=32$  Gbaud
  - ▶ 128G PM-QPSK
  - ▶ 256G PM-16QAM
- ▶ Nyquist-WDM
  - ▶ DSP spectral shaping
    - ▶ roll-off=0.02
  - ▶  $\Delta f=33.6$  GHz
- ▶ WDM
  - ▶ 9 channels

## RECEIVER

- ▶ Coherent receiver
- ▶ Electrical bandwidth
  - ▶  $B_{\text{elt}}=0.5 \cdot R_S=16.0$  GHz
- ▶ ADC
  - ▶ 2 SpS
- ▶ DSP
  - ▶ LMS with training sequence
  - ▶ 51 taps



## SMF

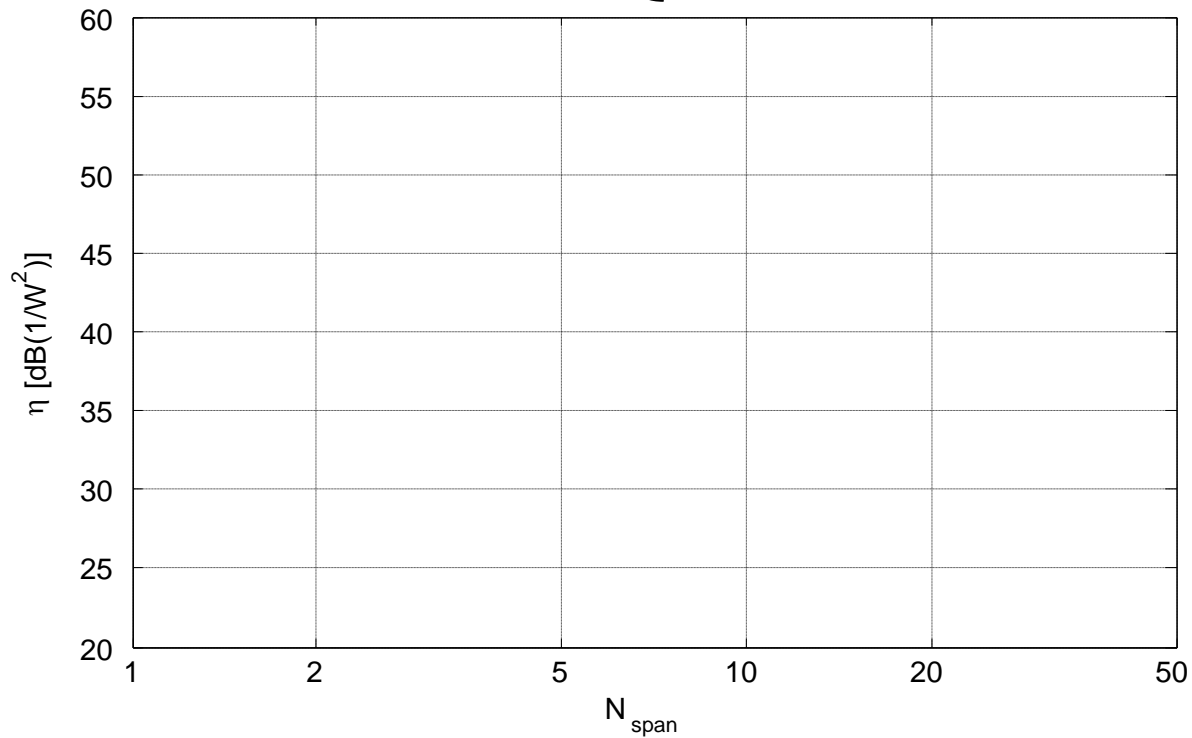
- Attenuation
  - $\alpha=0.2$  [dB/km]
- Non-linearity
  - $\gamma=1.3$  [1/W/km]
- Dispersion
  - $D=16.7$  [ps/nm/km]

## NZDSF

- Attenuation
  - $\alpha=0.22$  [dB/km]
- Non-linearity
  - $\gamma=1.5$  [1/W/km]
- Dispersion
  - $D=3.8$  [ps/nm/km]



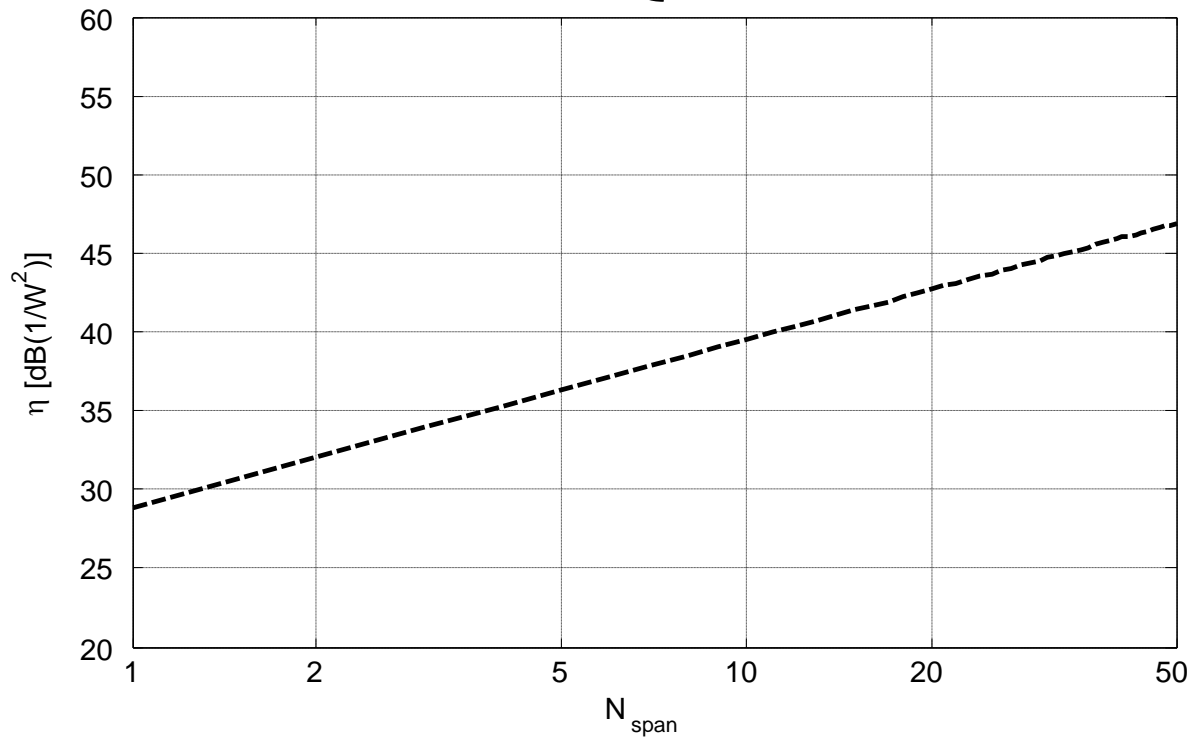
# PM-QPSK







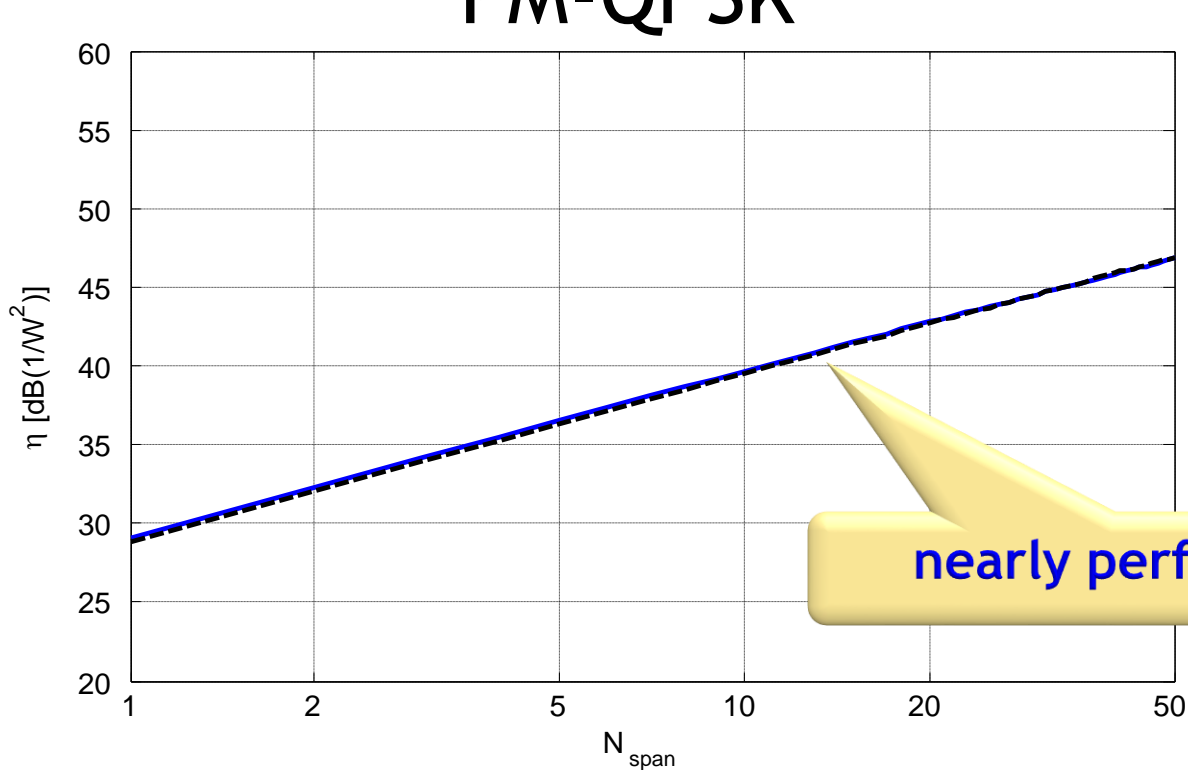
# PM-QPSK



Black dashed:  
Coherent  
GN-model



# PM-QPSK

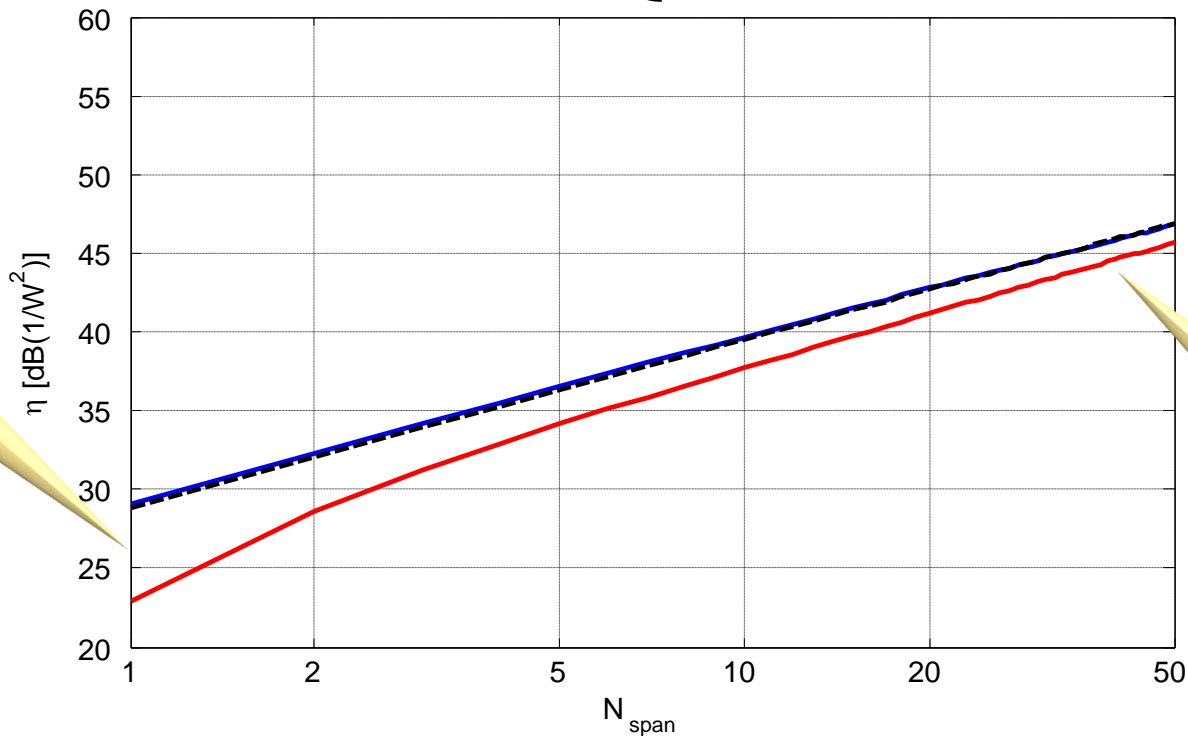


Black dashed:  
Coherent  
GN-model

Blue solid:  
Simulation with PD  
(+200,000 ps/nm)

nearly perfect match

# PM-QPSK



Black dashed:  
Coherent  
GN-model

Blue solid:  
Simulation with PD  
(+200,000 ps/nm)

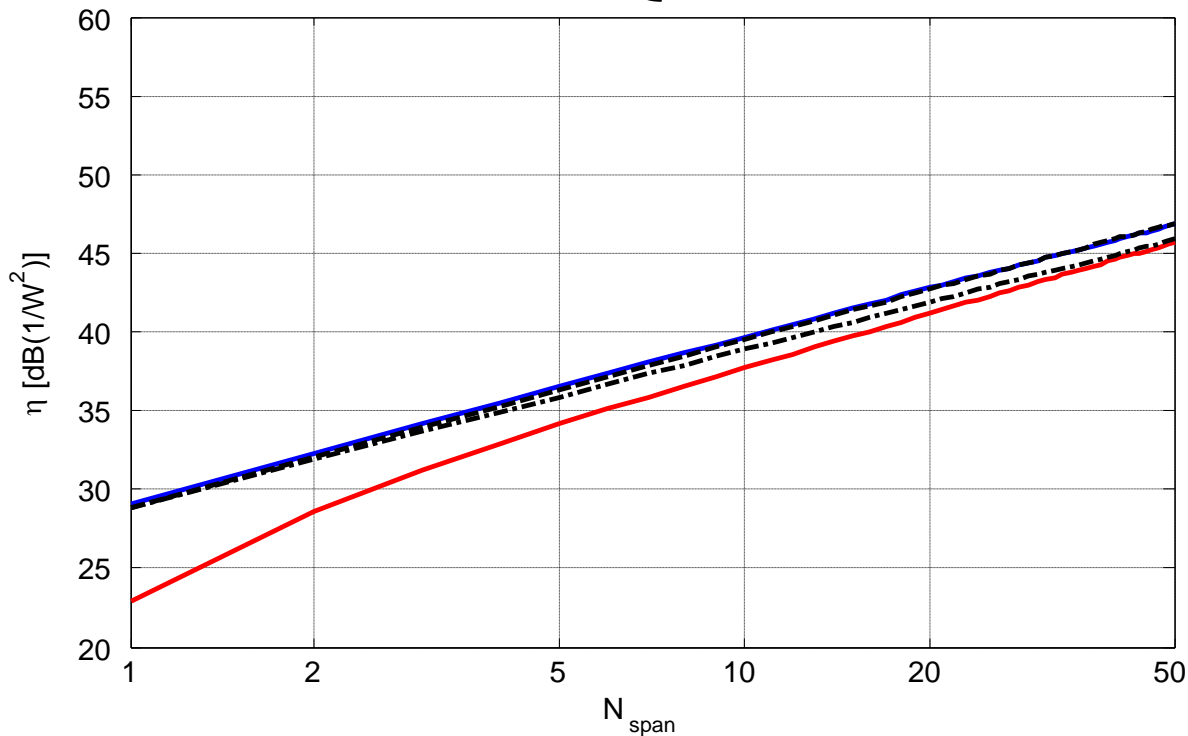
Red solid:  
Simulation NOPD

6 dB gap  
after 1  
span

<1.5 dB gap  
at Max Reach



# PM-QPSK



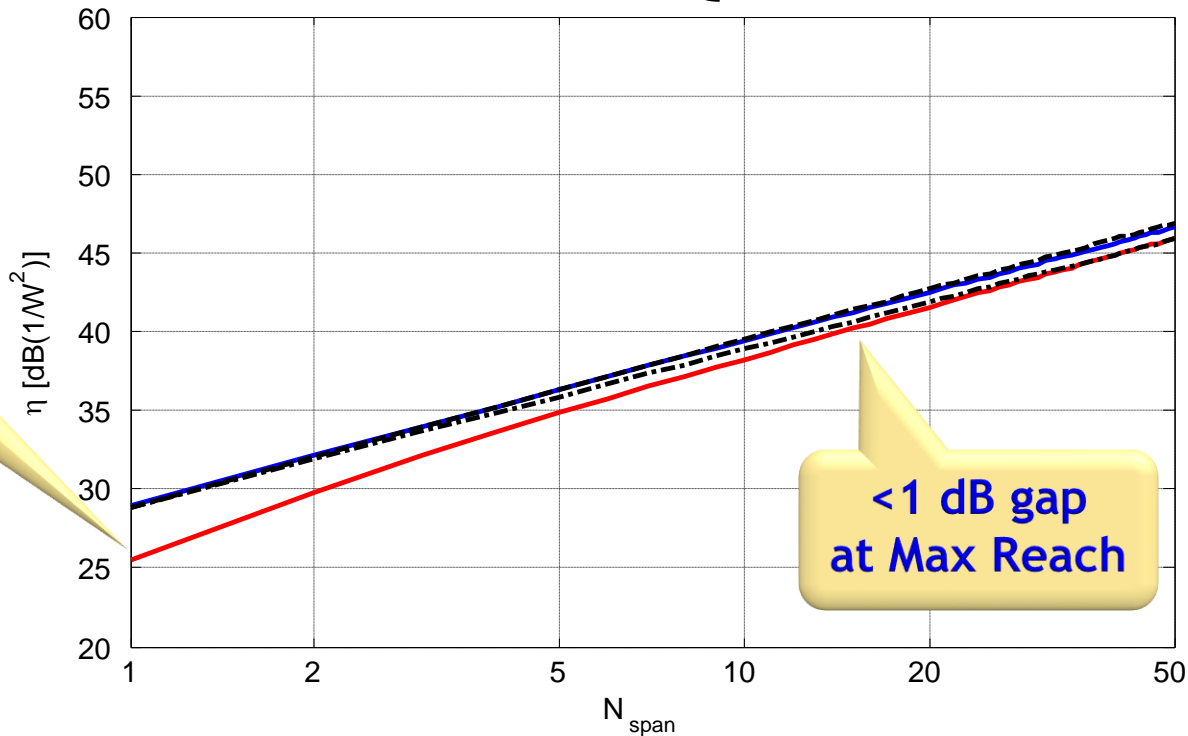
Black dashed:  
Coherent  
GN-model

Blue solid:  
Simulation with PD  
(+200,000 ps/nm)

Red solid:  
Simulation NOPD

Black dash-dotted:  
Incoherent  
GN-model

# PM-16QAM



3 dB gap  
after 1  
span

< 1 dB gap  
at Max Reach

Black dashed:  
Coherent  
GN-model

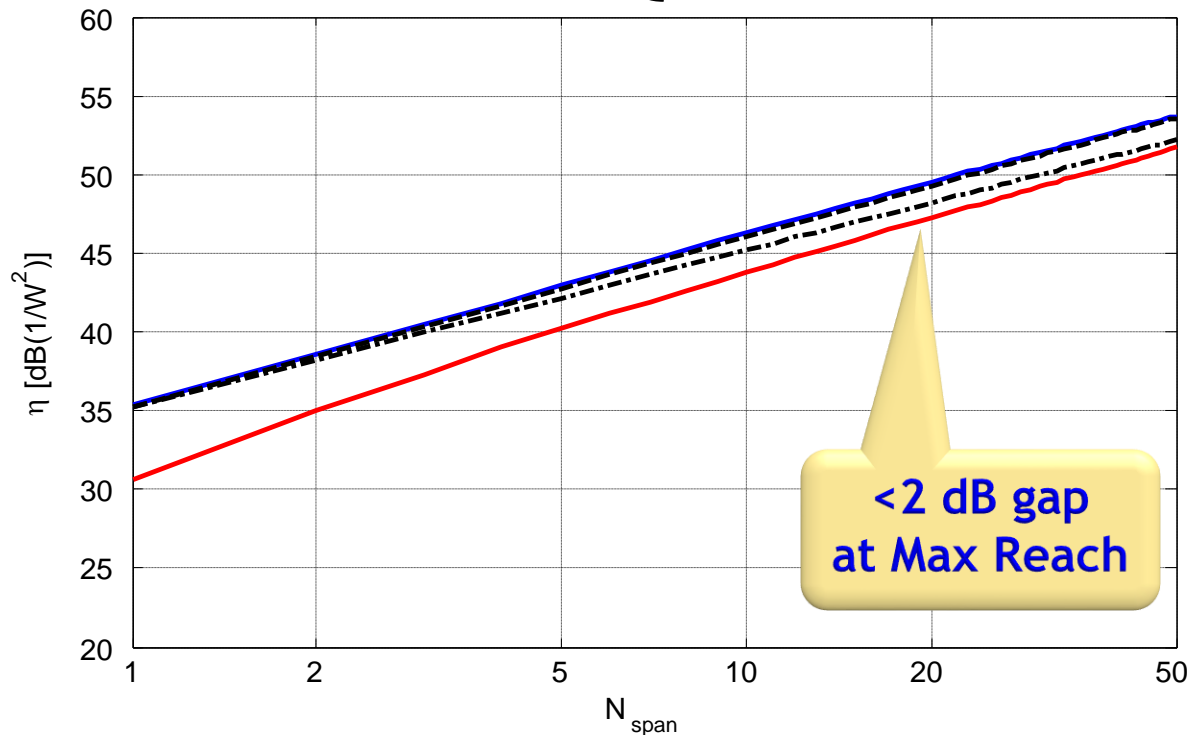
Blue solid:  
Simulation with PD  
(+200,000 ps/nm)

Red solid:  
Simulation NOPD

Black dash-dotted:  
Incoherent  
GN-model



## PM-QPSK



Black dashed:  
Coherent  
GN-model

Blue solid:  
Simulation with PD  
(+200,000 ps/nm)

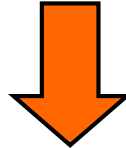
Red solid:  
Simulation NOPD

Black dash-dotted:  
Incoherent  
GN-model

<2 dB gap  
at Max Reach



$$N_{span,MAX} \propto \sqrt[3]{\frac{1}{\eta}}$$



$$\Delta N_{span,dB} = -\frac{1}{3} \Delta \eta_{dB}$$

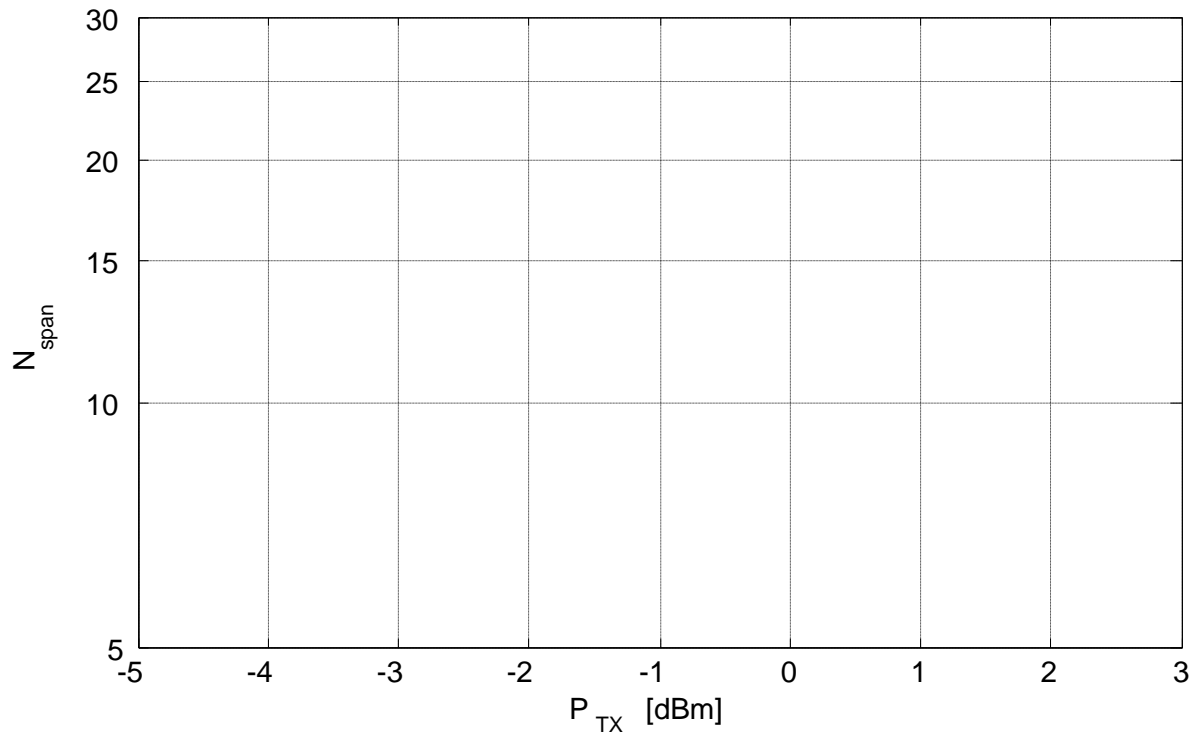
Inaccuracies in  $\eta$  estimation are mitigated by 1/3



# System impact



$$\text{BER}_{\text{target}} = 10^{-3}$$



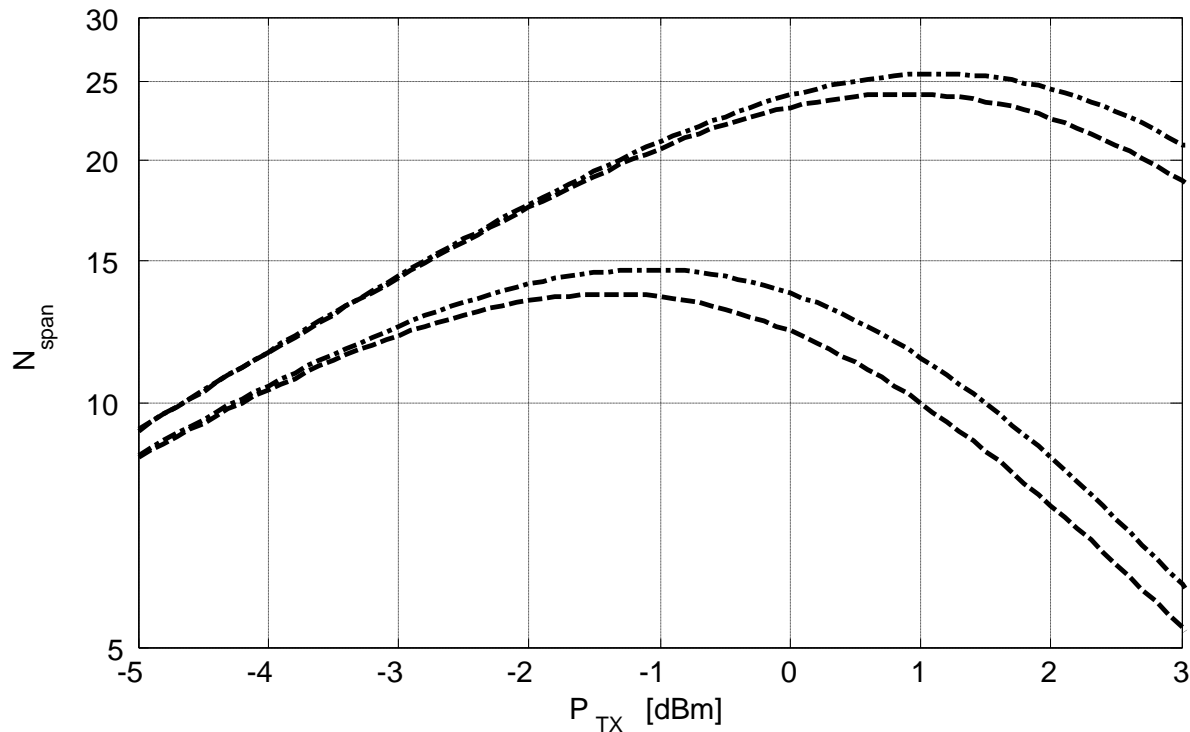
PM-QPSK  
 $L_{\text{span}} = 110$  km

PM-16QAM  
 $L_{\text{span}} = 80$  km





$BER_{\text{target}} = 10^{-3}$



PM-QPSK  
 $L_{\text{span}} = 110$  km

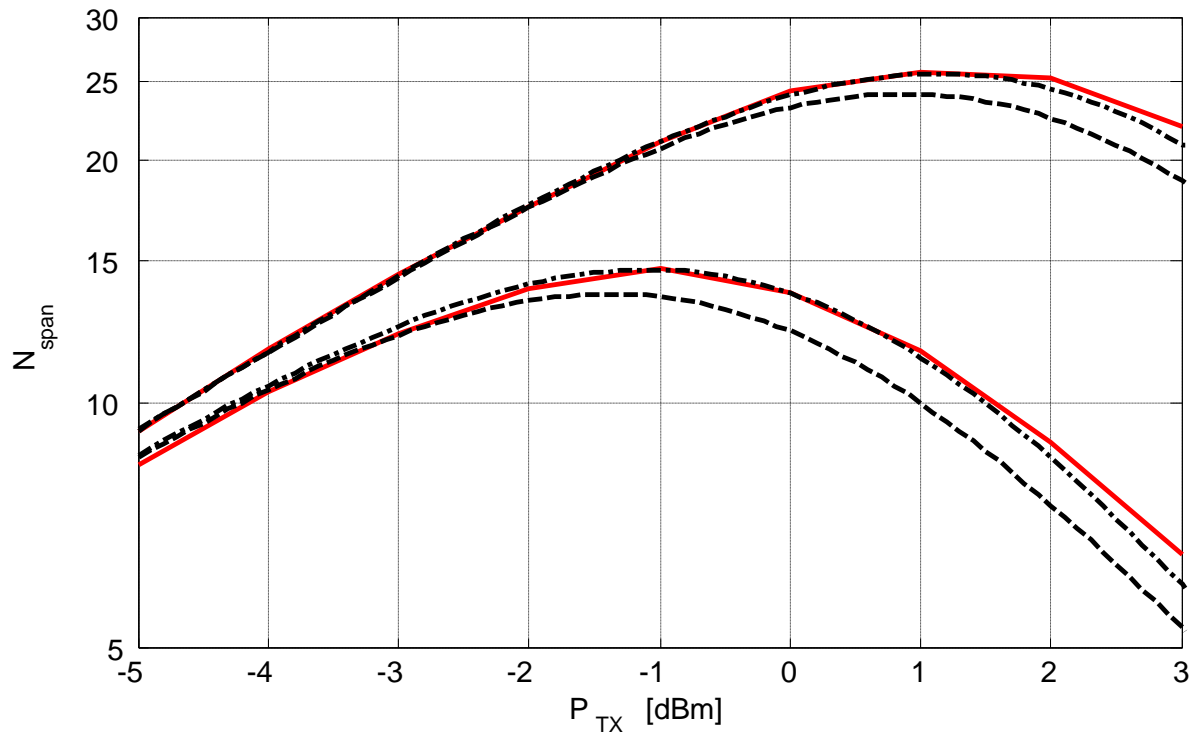
PM-16QAM  
 $L_{\text{span}} = 80$  km

Black dashed:  
Coherent  
GN-model

Black dash-dotted:  
Incoherent  
GN-model



$BER_{\text{target}} = 10^{-3}$



PM-QPSK  
 $L_{\text{span}} = 110$  km

PM-16QAM  
 $L_{\text{span}} = 80$  km

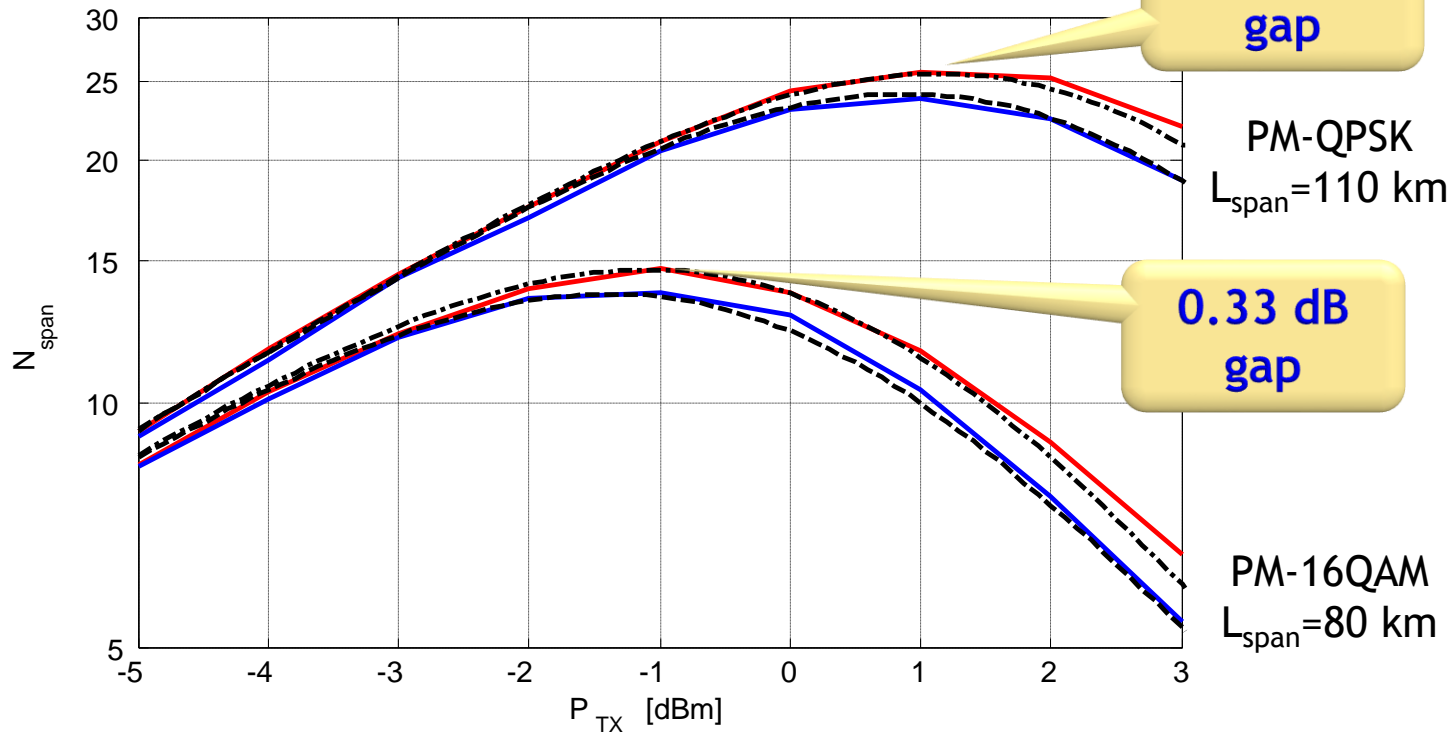
Black dashed:  
Coherent  
GN-model

Black dash-dotted:  
Incoherent  
GN-model

Red solid:  
Simulation NOPD



$BER_{\text{target}} = 10^{-3}$



Black dashed:  
Coherent  
GN-model

Black dash-dotted:  
Incoherent  
GN-model

Red solid:  
Simulation NOPD

Blue solid:  
Simulation with PD  
(+200,000 ps/nm)



- ▶ The Initial Dispersion Transient does have some impact on the accuracy of the GN-model
- ▶ With QAM constellations, the Coherent GN-model always provides a lower bound to system performances
  - ▶ High-order constellations show better accuracy because they are closer to Gaussian distribution already at transmitter (higher PAPR)
- ▶ The Incoherent GN-model typically delivers good prediction
  - ▶ It is not a more faithful modeling, two approximations tend to cancel each other out



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